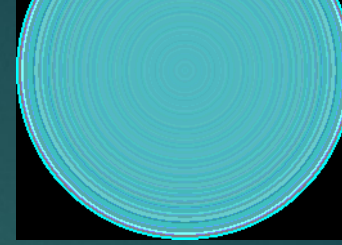
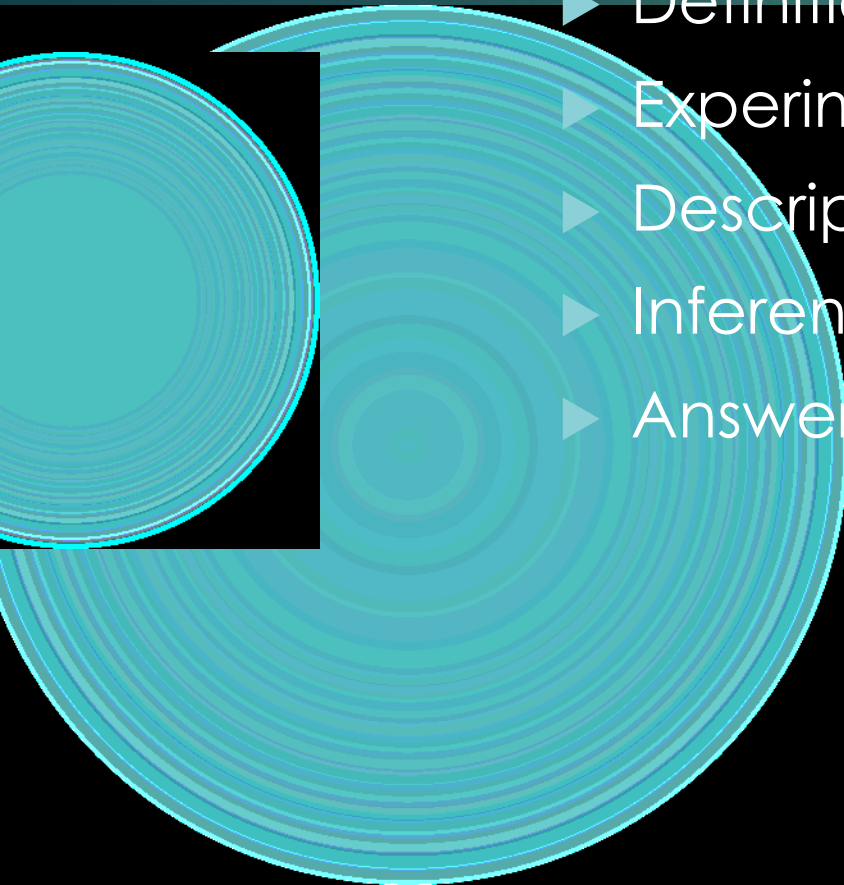


Flowchart



1

- ▶ Question
- ▶ Definition of sample population
- ▶ Experiments and data collection
- ▶ Descriptive statistics
- ▶ Inferential statistics
- ▶ Answering the question

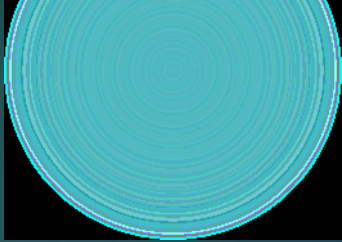





CONFIDENCE INTERVAL

2

CONFIDENCE INTERVALS CONSIST OF A RANGE OF VALUES (INTERVAL) THAT ACT AS GOOD ESTIMATES OF THE UNKNOWN POPULATION PARAMETER.

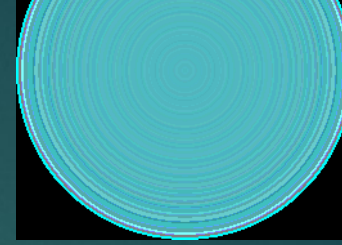


- 
- 
- 
- 
- ▶ The desired level of confidence is set by the researcher (**not determined by data**). Most commonly, the 95% confidence level is used. However, other confidence levels can be used, for example, 90% and 99%.
- 

- WE KNOW THE VARIANCE (σ^2) OF THE POPULATION (FOR EXAMPLE FROM PREVIOUS SURVEYS)

- WE DO NOT KNOW THE VARIANCE OF THE POPULATION (MOST FREQUENT CASE)

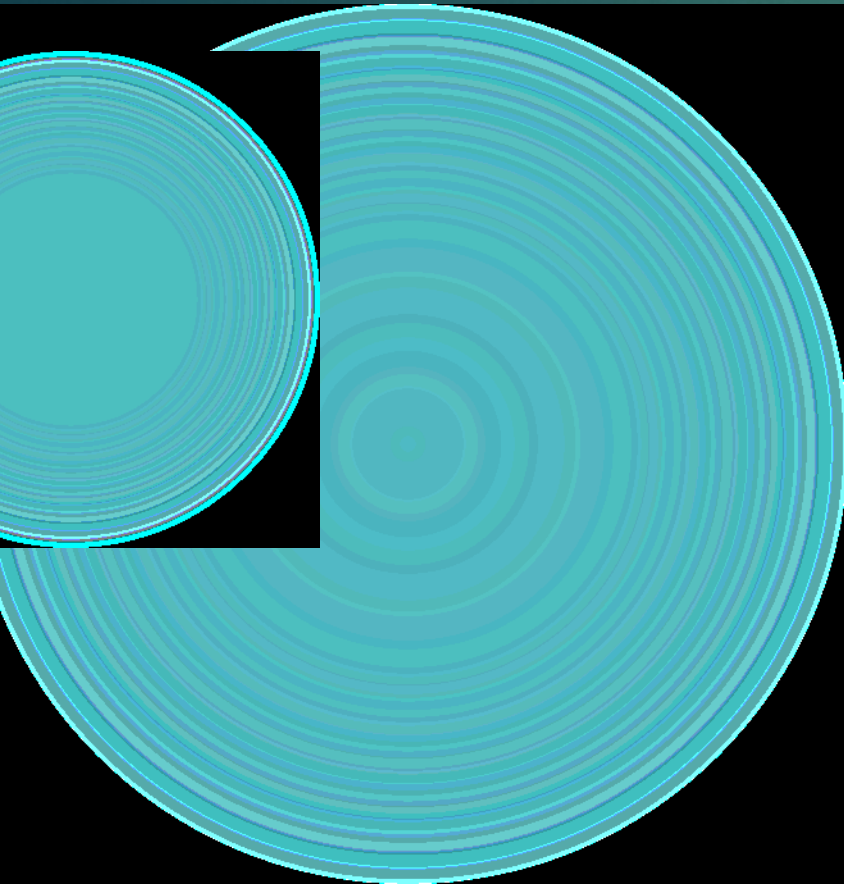
Esempio



5

CASE 1:

EXCEL: =CONFIDENZA(A; Σ ; DIMENSIONI CAMPIONE)



Caso 2

6

ESAMINO 240 TOPINI E TROVO CHE IL 35 HANNO UNA MUTAZIONE XYZ DI MIO INTERESSE. QUALE SARÀ LA STIMA DELLA PERCENTUALE DI TOPI AFFETTI, CON UN IC DEL 95%?

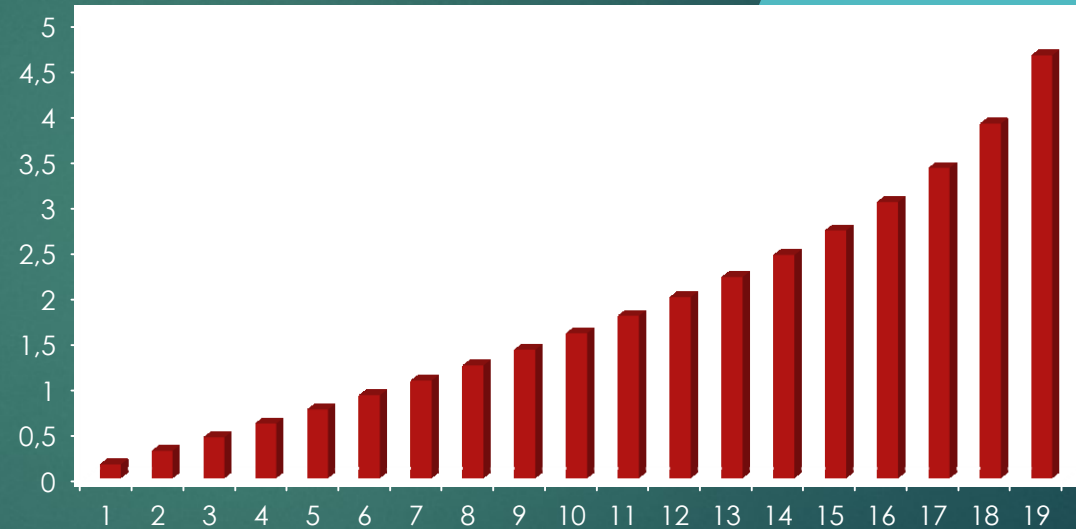
$$\text{Frequenza } \pm 1.96 * \sqrt{\frac{\text{affetti} * (1 - \text{affetti})}{N}}$$

% affetti = 14,58
% non affetti = 85,41
N = 240

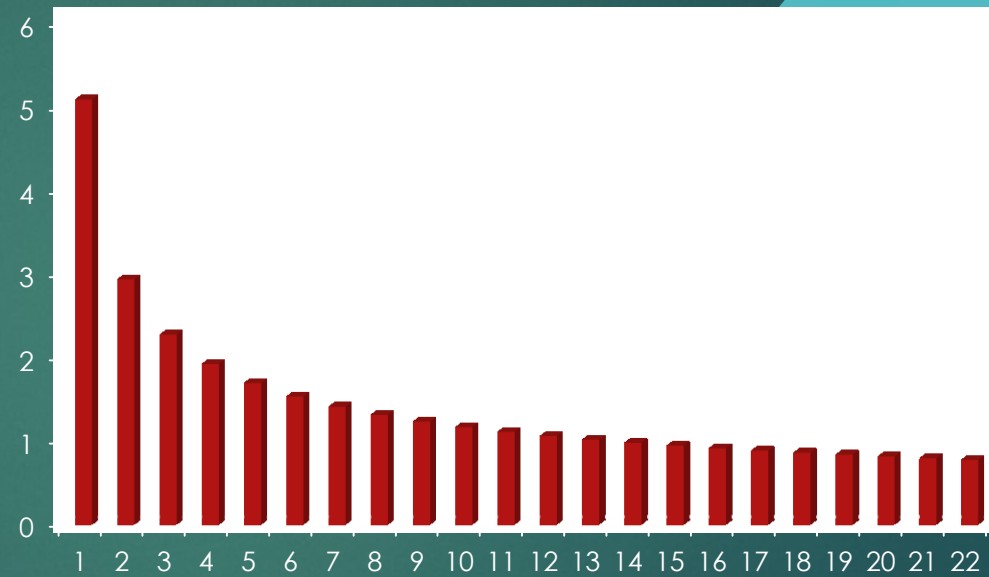
% compresa tra **30,53**
39,46

Some considerations...

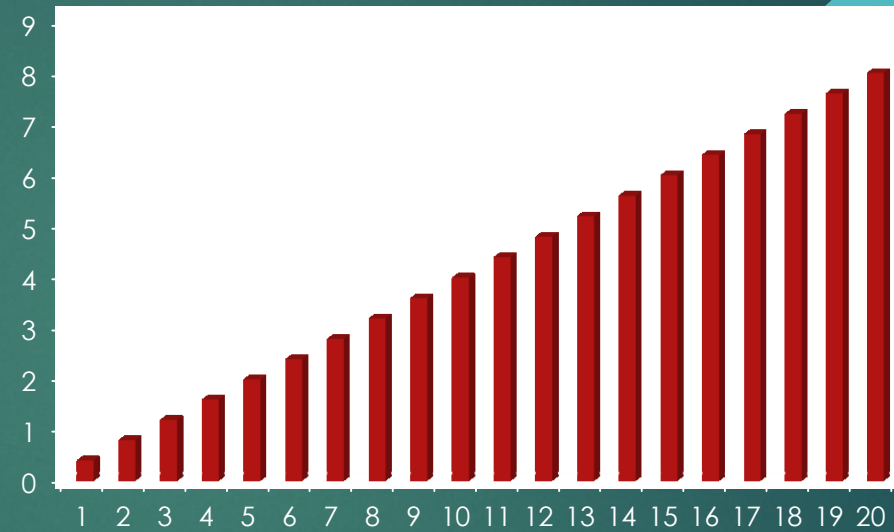
alfa	dev st	numerosità	intervallo
1	5,8	24	
0,95	5,8	24	0,14848
0,9	5,8	24	0,297546
0,85	5,8	24	0,447802
0,8	5,8	24	0,599885
0,75	5,8	24	0,754487
0,7	5,8	24	0,912377
0,65	5,8	24	1,074436
0,6	5,8	24	1,241697
0,55	5,8	24	1,4154
0,5	5,8	24	1,597084
0,45	5,8	24	1,788702
0,4	5,8	24	1,992824
0,35	5,8	24	2,212958
0,3	5,8	24	2,454109
0,25	5,8	24	2,723843
0,2	5,8	24	3,034509
0,15	5,8	24	3,40858
0,1	5,8	24	3,89475
0,05	5,8	24	4,640881
-3,2E-16	5,8	24	



alfa	dev st	numerosità	intervallo confidenza
0,05	5,8	5	5,083831
0,05	5,8	15	2,935151
0,05	5,8	25	2,273558
0,05	5,8	35	1,921507
0,05	5,8	45	1,69461
0,05			1,532833
0,05			1,410001
0,05	5,8		1,312639
0,05	5,8		1,23301
0,05	5,8		1,166311
0,05	5,8		1,109383
0,05	5,8	11	1,060052
0,05	5,8	125	1,016766
0,05	5,8	135	0,978384
0,05	5,8	145	0,944044
0,05	5,8	155	0,913083
0,05	5,8	165	0,884981
0,05	5,8	175	0,859324
0,05	5,8	185	0,835777
0,05	5,8	195	0,814064
0,05	5,8	205	0,793961
0,05	5,8	215	0,775277

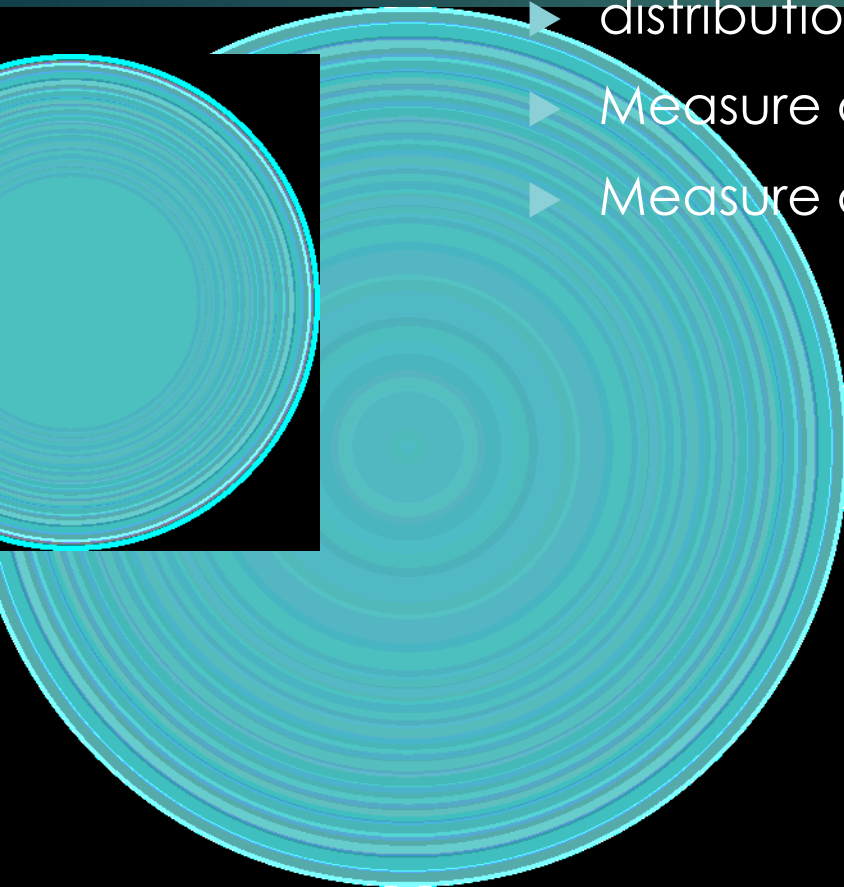


alfa	dev st	numerosità	intervallo confidenza
0,05	1	24	0,400076
0,05	2	24	0,800152
0,05	3	24	1,200228
0,05	4	24	1,600304
0,05	5	24	2,00038
0,05	6	24	2,400456
0,05	7	24	2,800532
0,05	8	24	3,200608
0,05	9	24	3,600684
0,05	10	24	4,00076
0,05	11	24	4,400836
0,05	12	24	4,800912
0,05	13	24	5,200988
0,05	14	24	5,601064
0,05	15	24	6,00114
0,05	16	24	6,401216
0,05	17	24	6,801292
0,05	18	24	7,201368
0,05	19	24	7,601443
0,05	20	24	8,001519

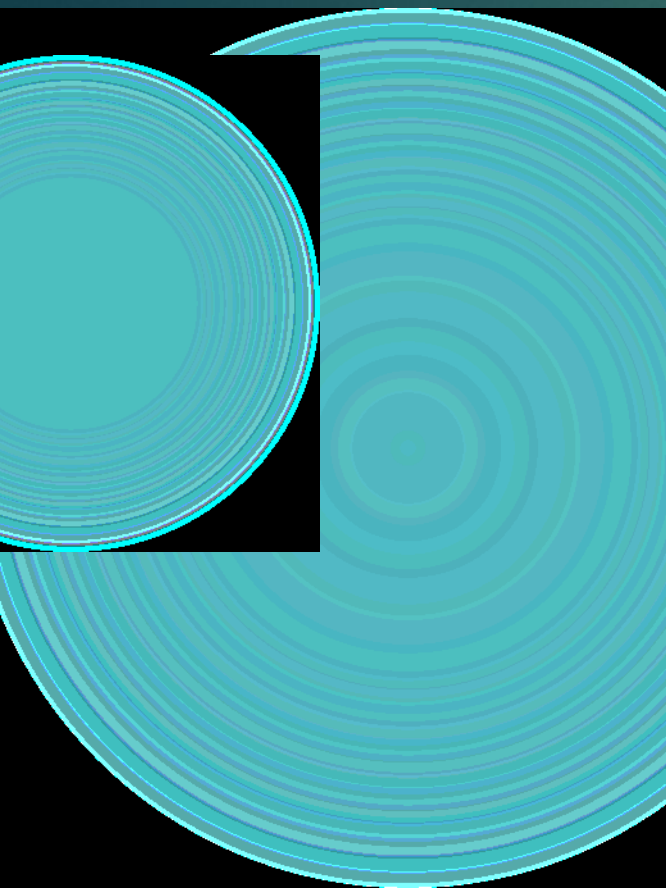
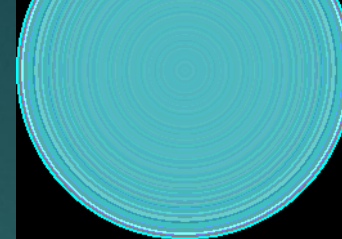


Descriptive statistics

- ▶ distribution
- ▶ Measure of central tendency
- ▶ Measure of variability



Yes or not experiments



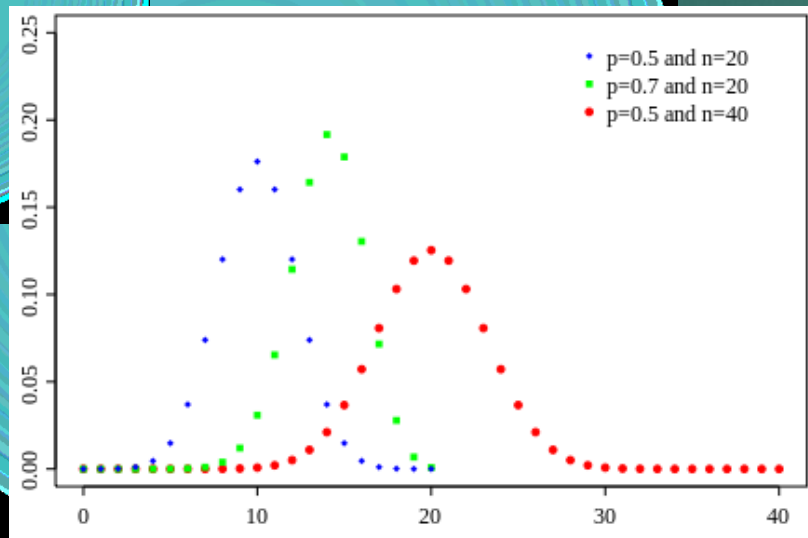
Binomial distribution

12



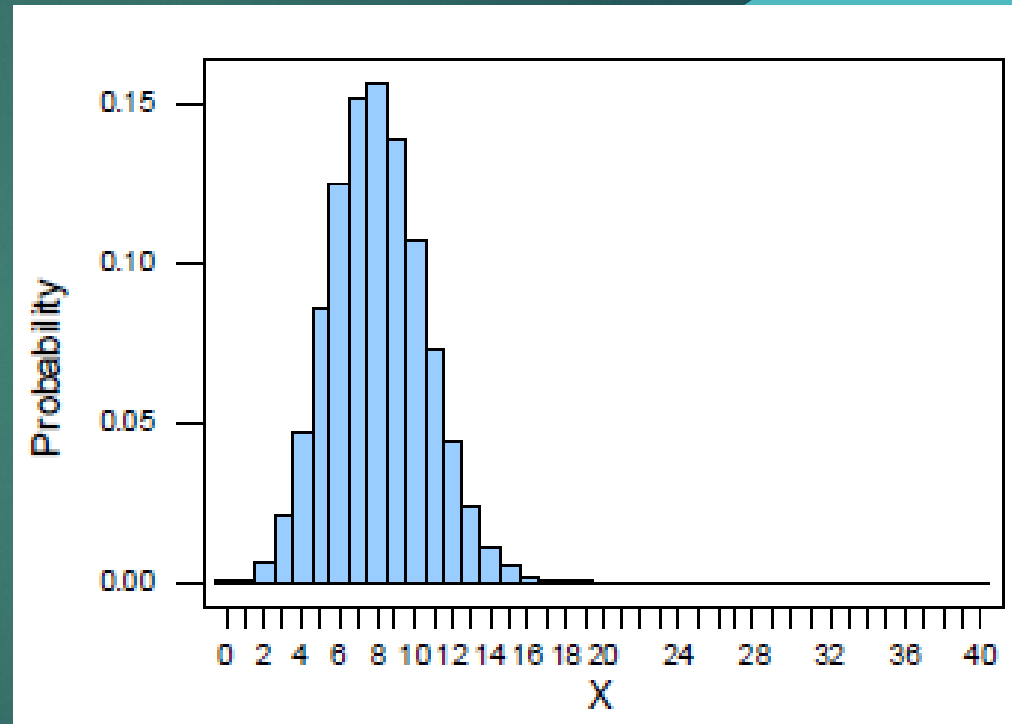
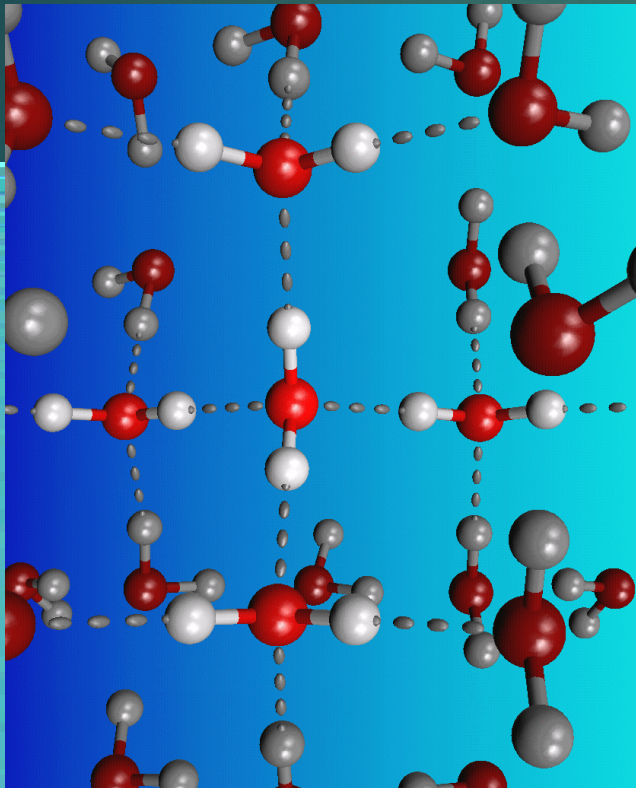
BERNOULLI'S EXPERIMENT: :

- 1) THE RESULT OF EACH TEST MAY BE ONLY "SUCCESS" OR "FAILURE";
- 2) THE RESULT OF EACH TEST IS INDEPENDENT OF THE RESULTS OF THE PREVIOUS TESTS;
- 3) THE PROBABILITY P OF "SUCCESS", AND HENCE THE PROBABILITY $Q = 1 - P$ OF "FAILURE", ARE CONSTANT IN EACH TRIAL.



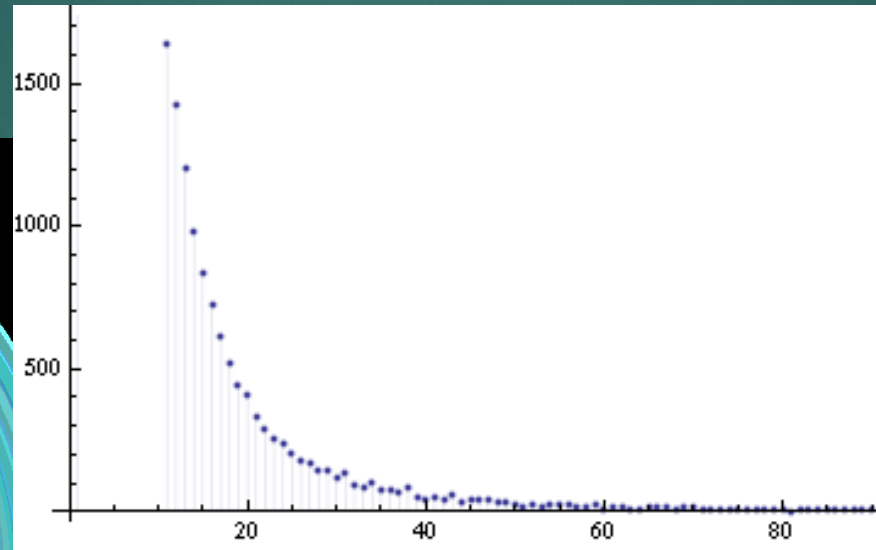
POISSON distribution

13



PARETO distribution

14

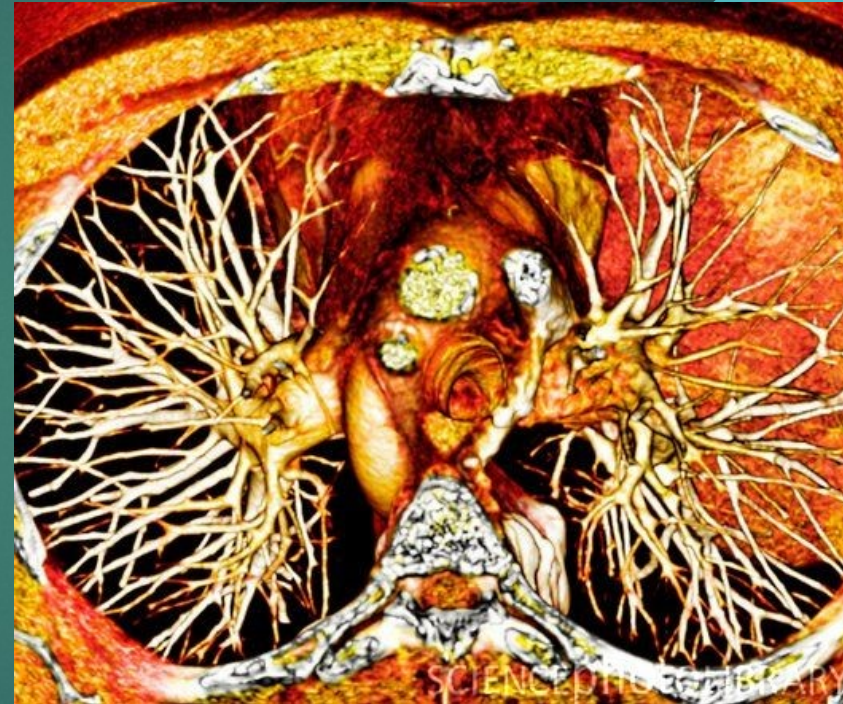
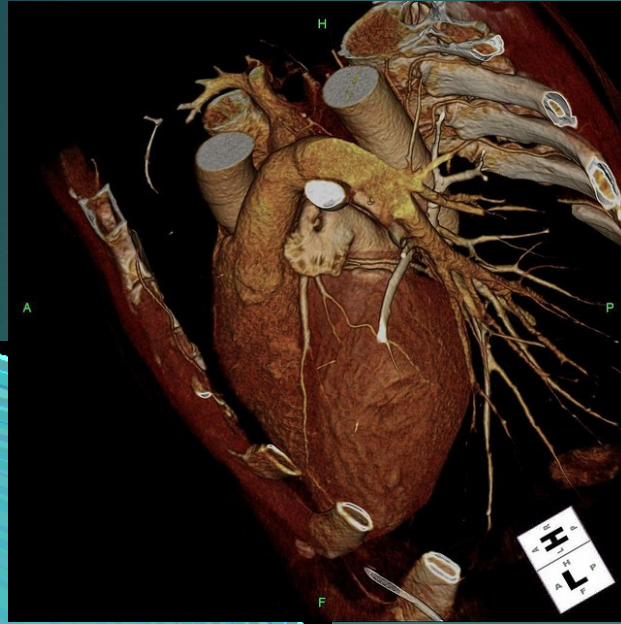
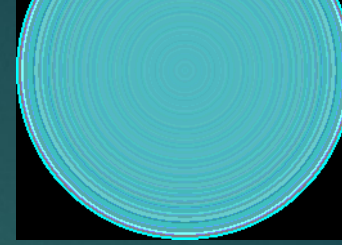


$$y = a x^{-b}$$

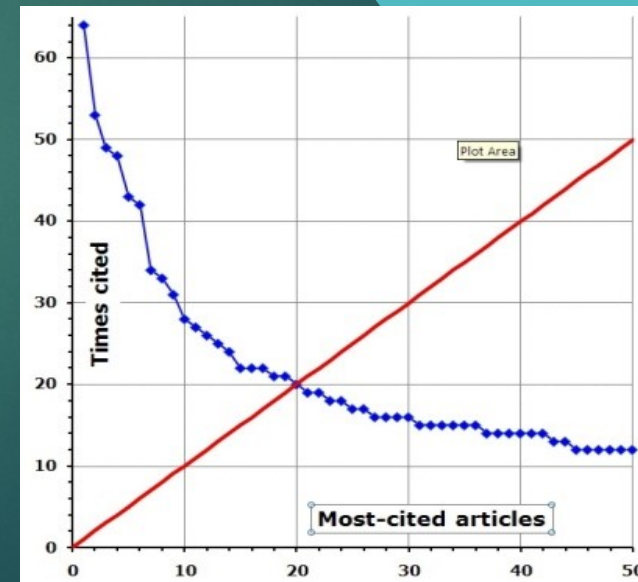
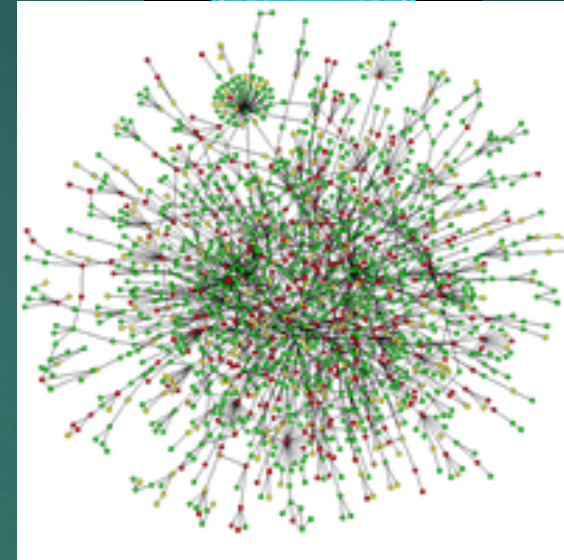
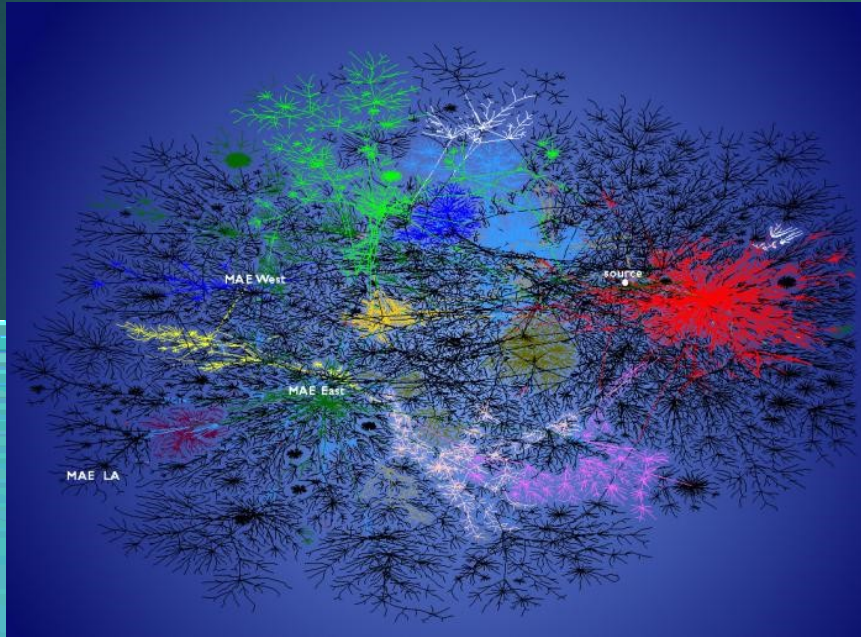
$$b > 1$$



PARETO distribution

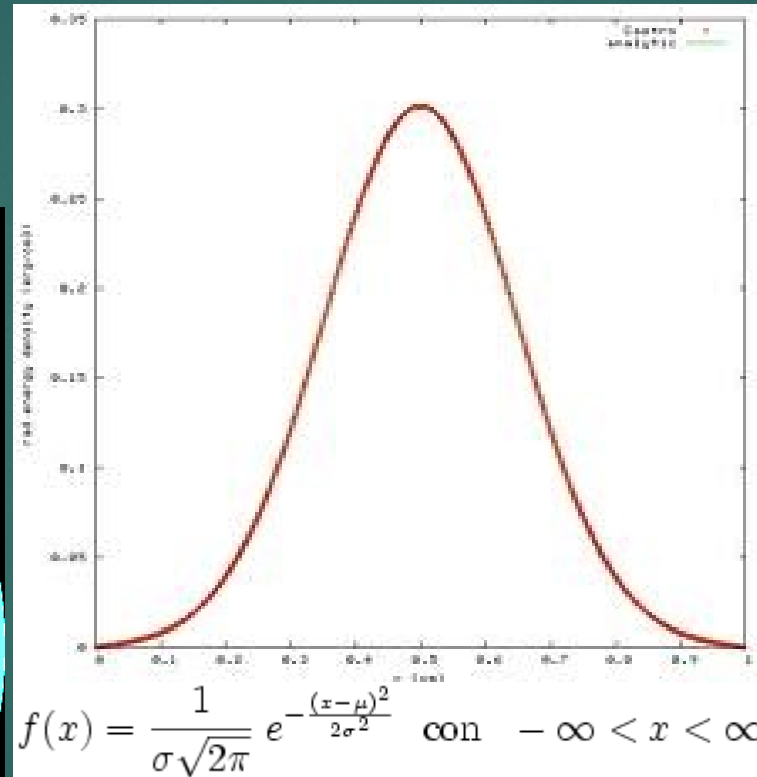


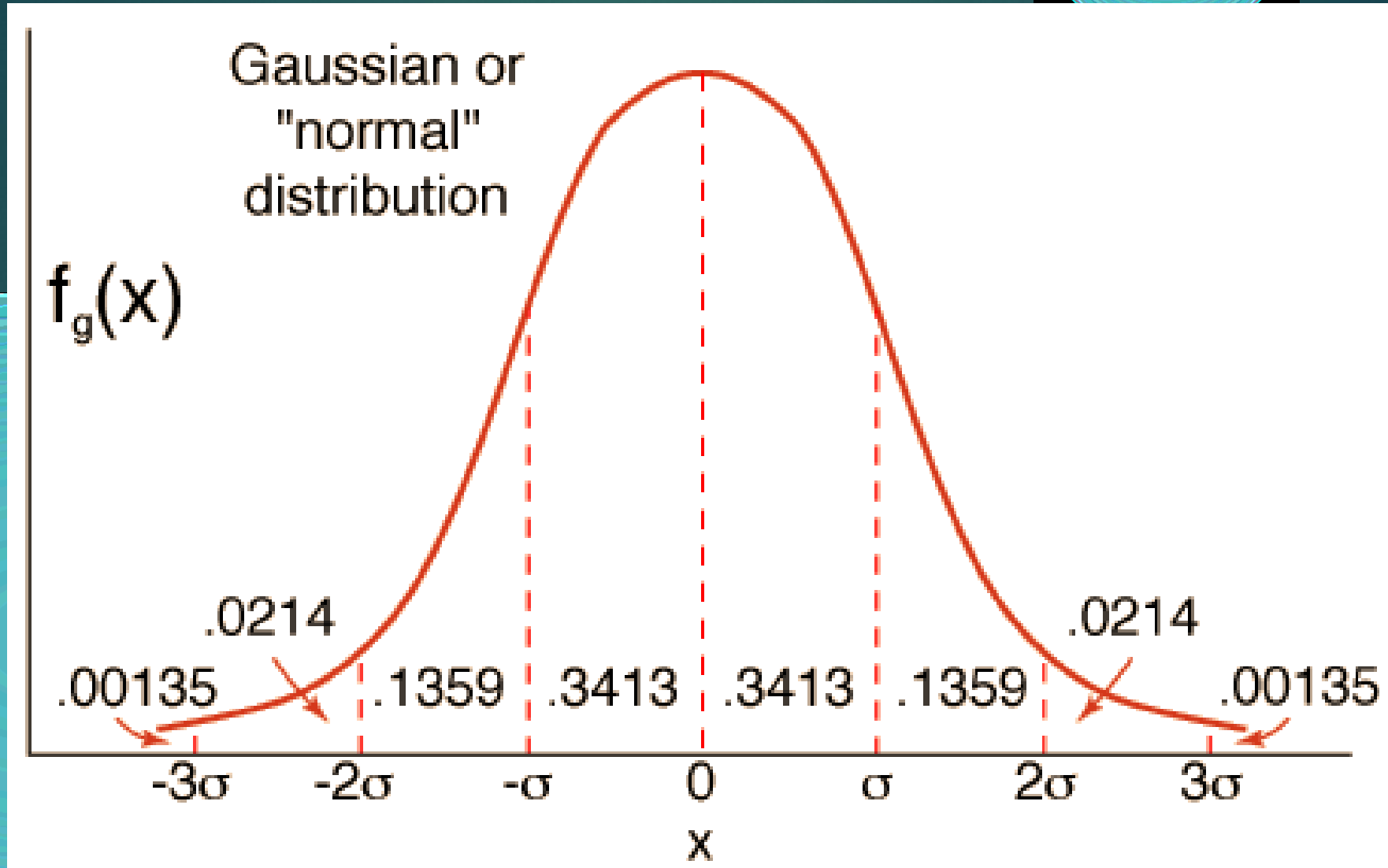
Scale free properties



GAUSSIAN distribution

17

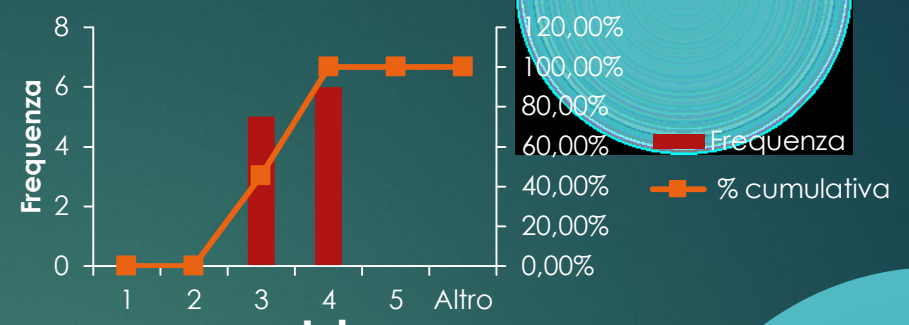




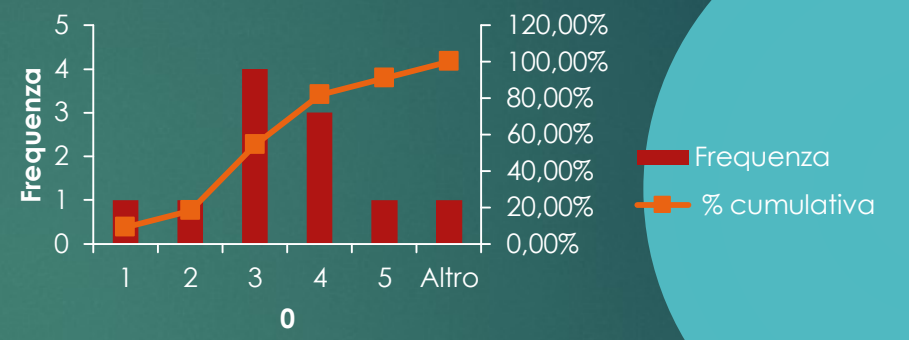
Weight		
A	B	C
3	2	0,5
4	3	1
3,3	4	2
4	3	3
3	3	4
3	4	5
3	4	6
3	4	7
3,5	2	2
3,3	3	3
3,4	4	4
3	1	4

media	3,318182	3,333333	3,409091
varianza	0,147636	1,878788	4,140909
dev. standard	0,384235	1,370689	2,034922
err. standard	0,03493	0,114224	0,184993

Istogramma



Istogramma

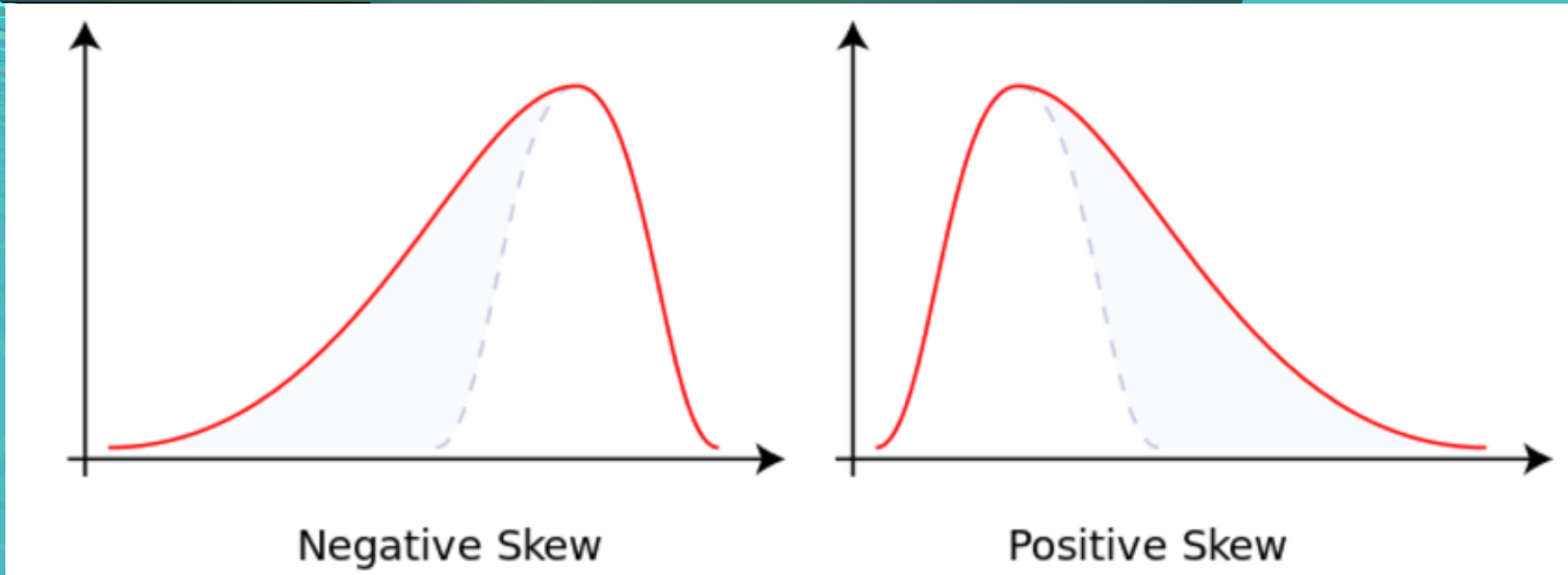


Istogramma

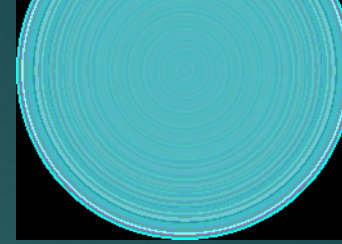


Skewness

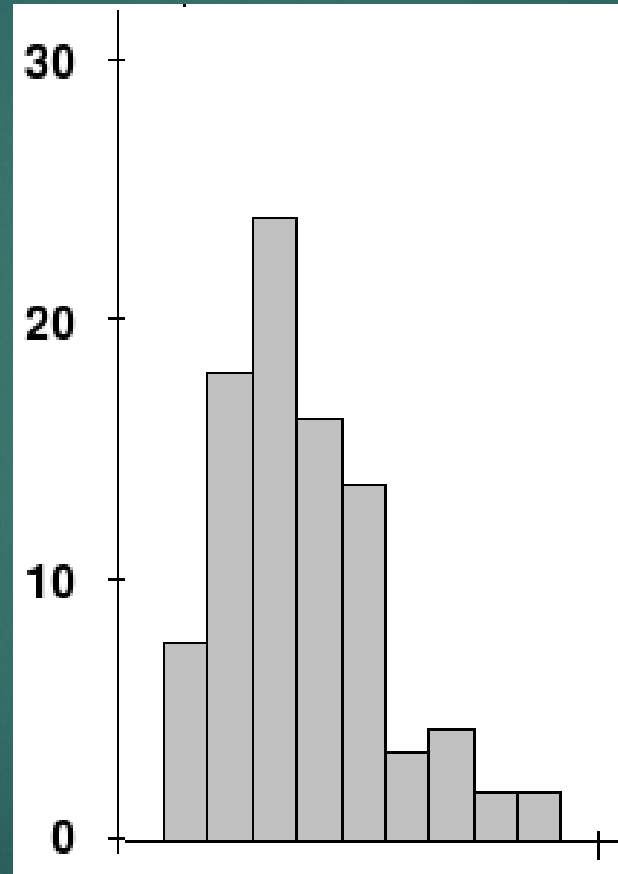
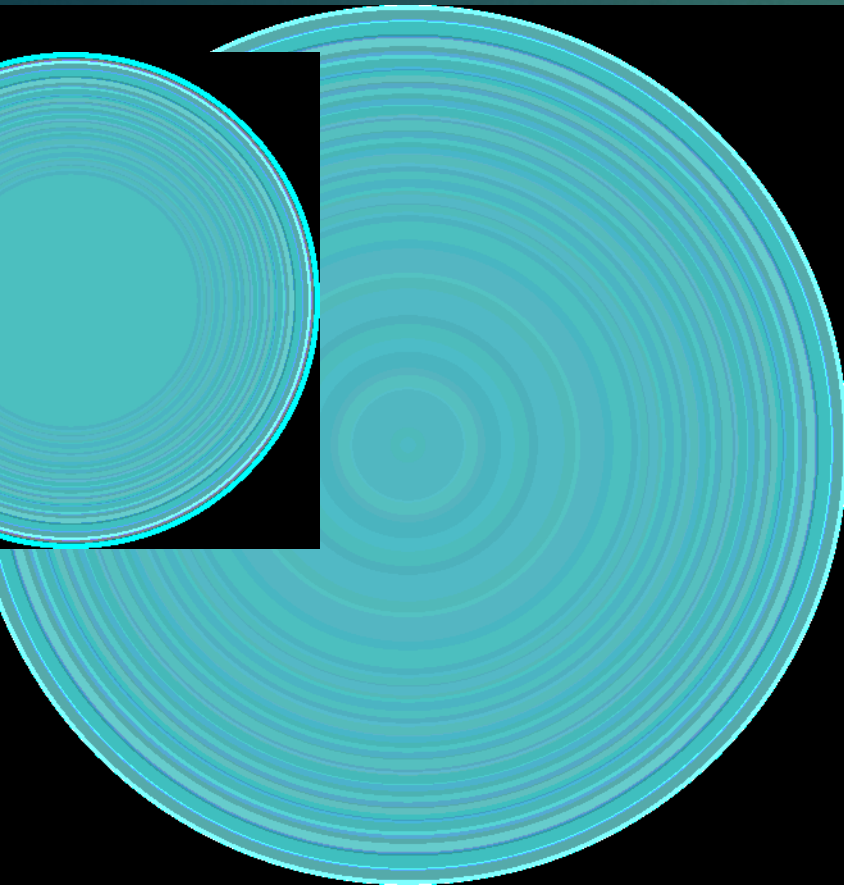
skewness is a measure of the asymmetry of the **probability distribution** of a **real-valued random variable** about its mean. The skewness value can be positive or negative, or undefined.



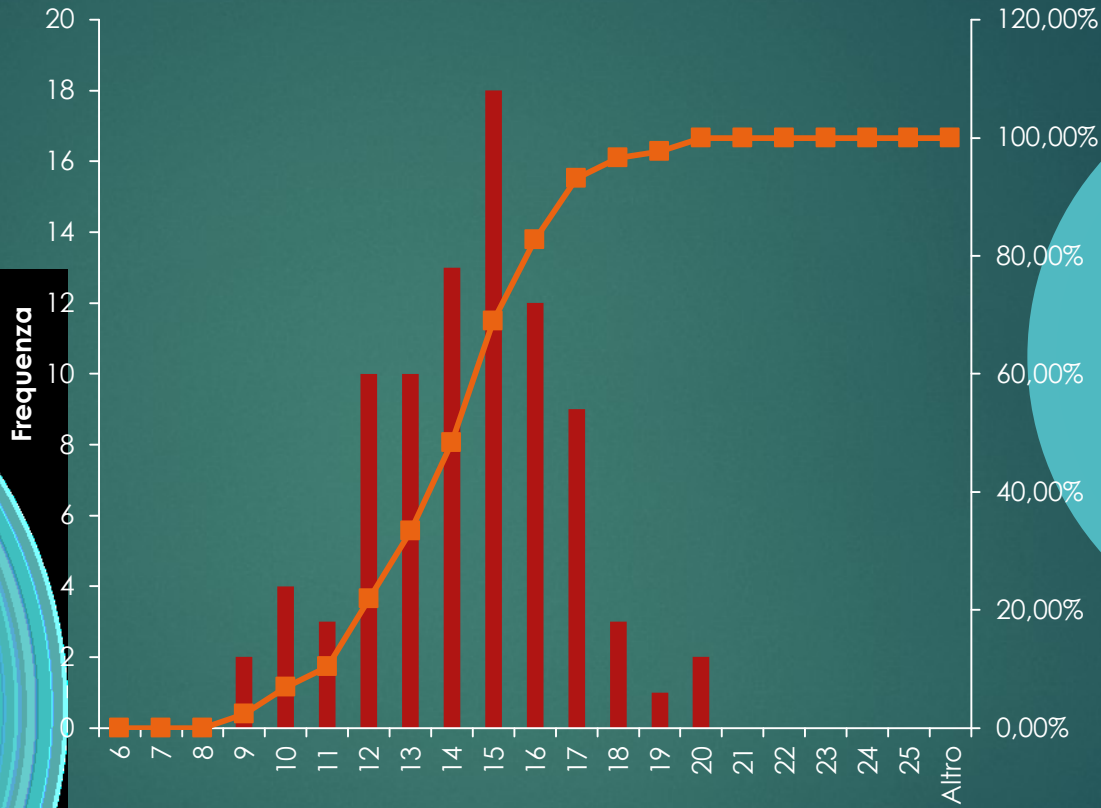
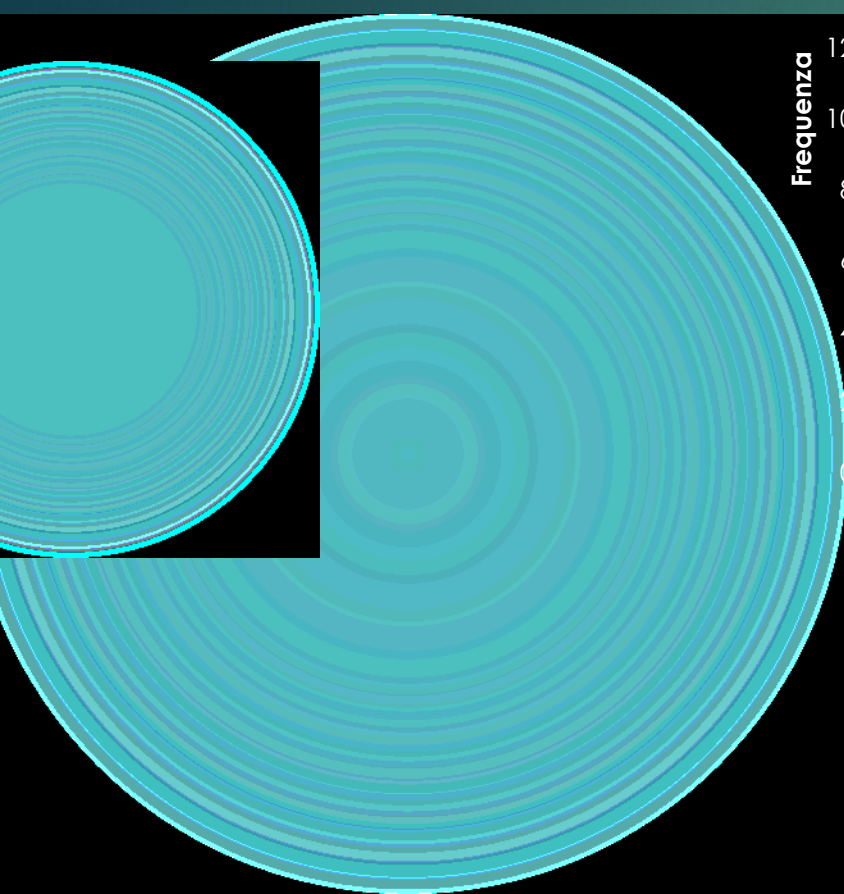
ASIMMETRY



21



Skewness



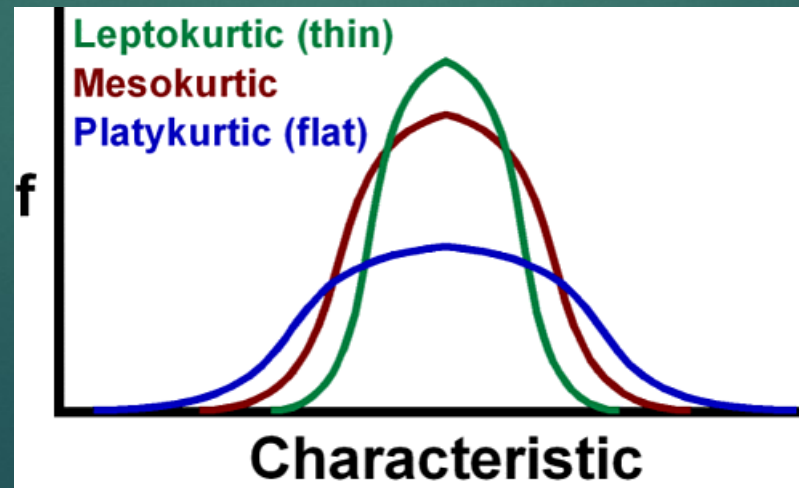
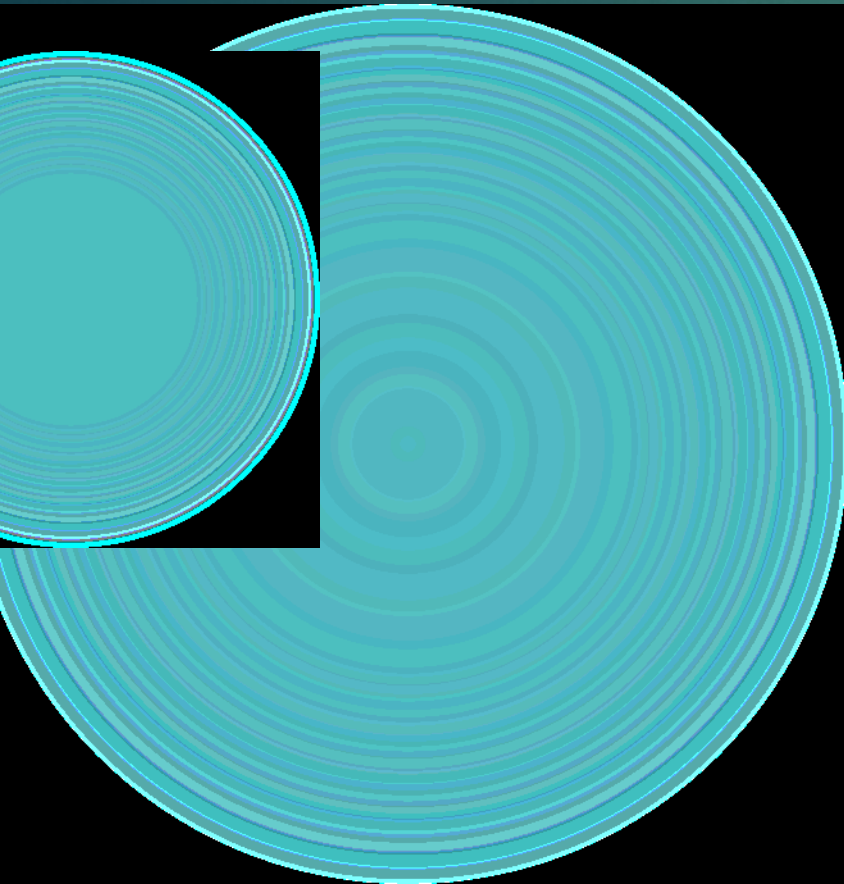
asimmetria = -0,08511



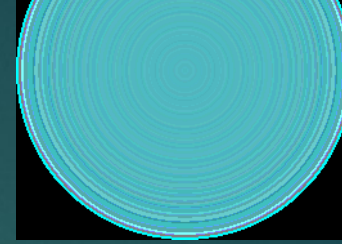
Kurtosis

23

- ▶ La **curtosi** (o **kurtosi**) è un **allontanamento dalla normalità distributiva**, rispetto alla quale si verifica un maggiore *appiattimento* (distribuzione platicurtica) o un maggiore *allungamento* (distribuzione leptocurtica).

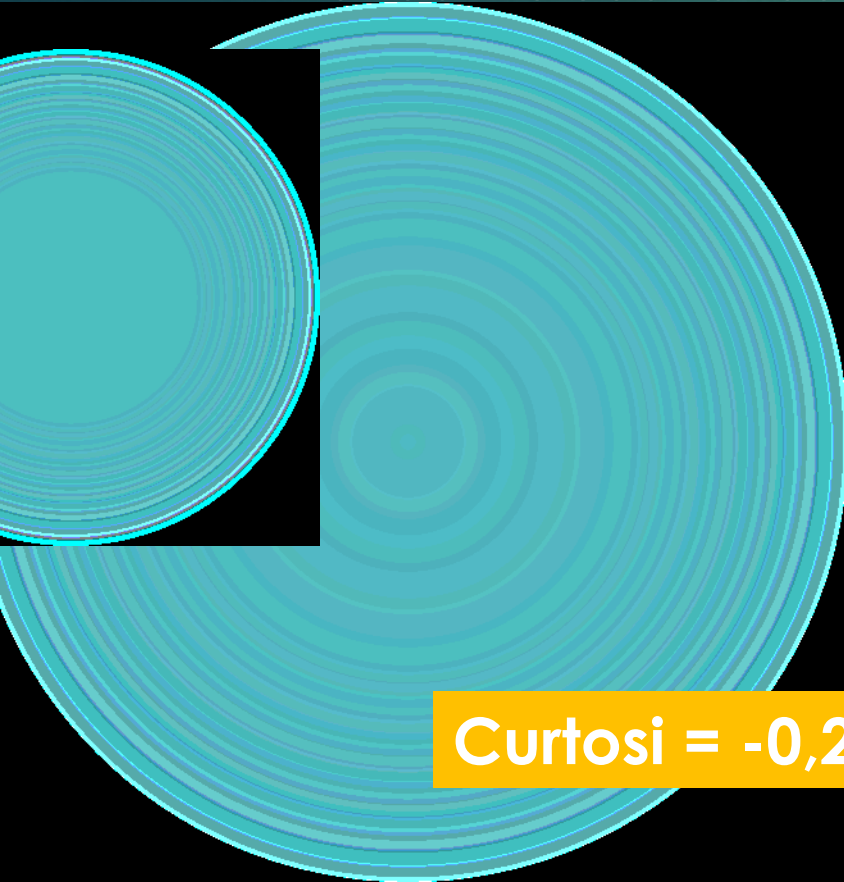


CURTOSI

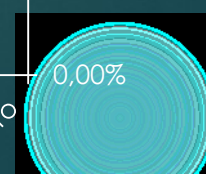
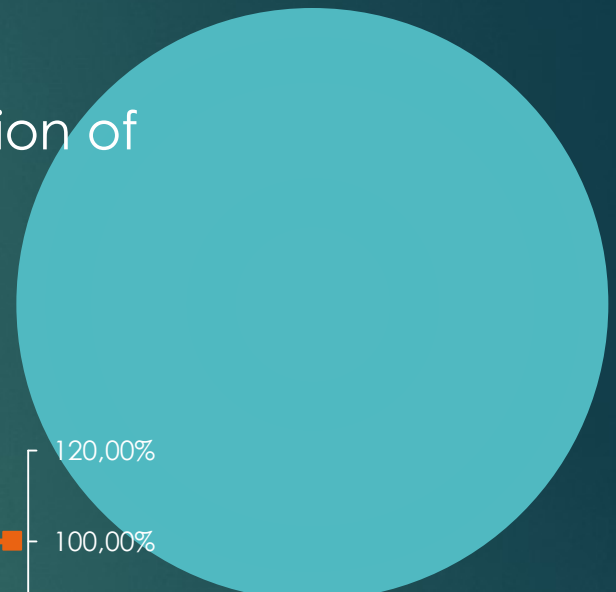
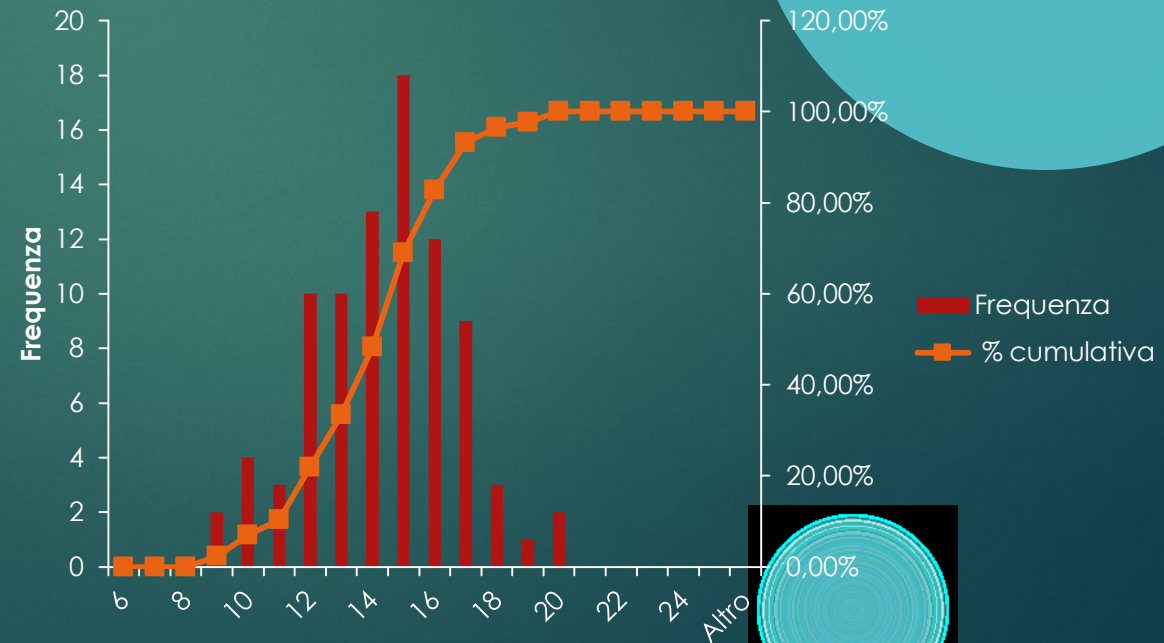


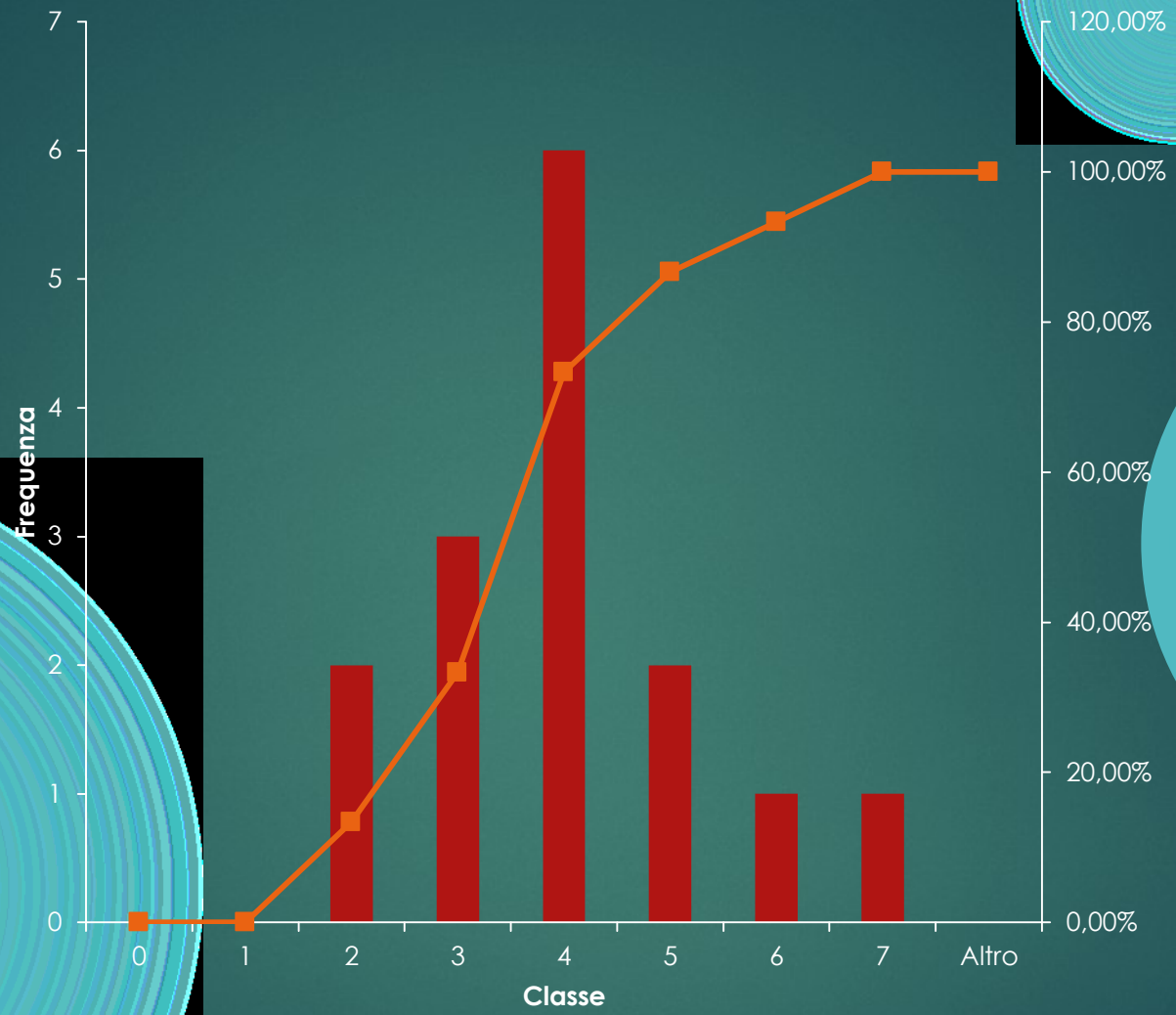
24

- ▶ is a measure of the "tailedness" of the probability distribution of a real-valued random variable.

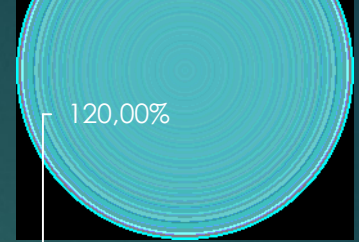
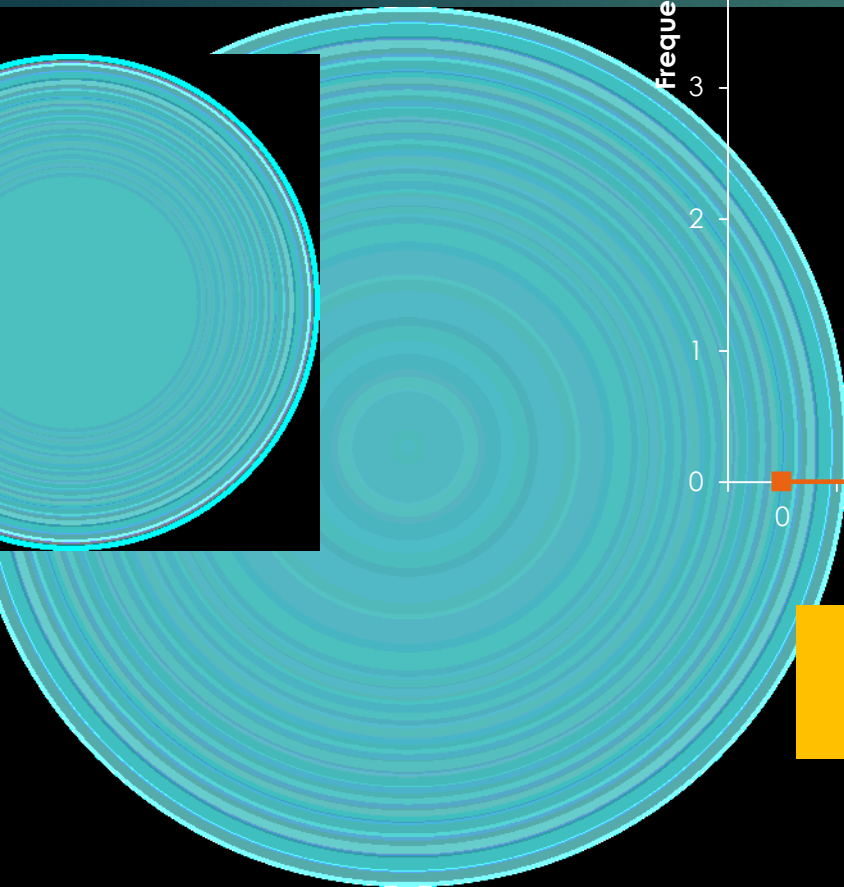


Curtosi = -0,26316



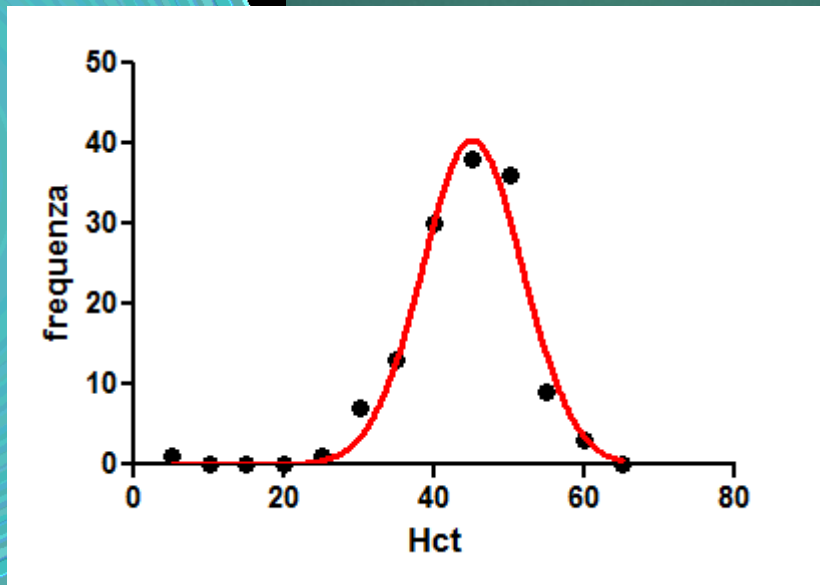
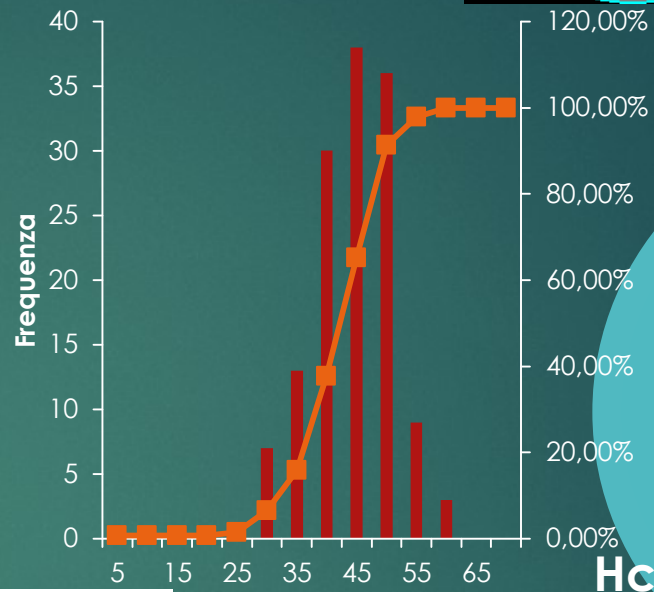


asimmetria 0,800298
curtosi 0,753757



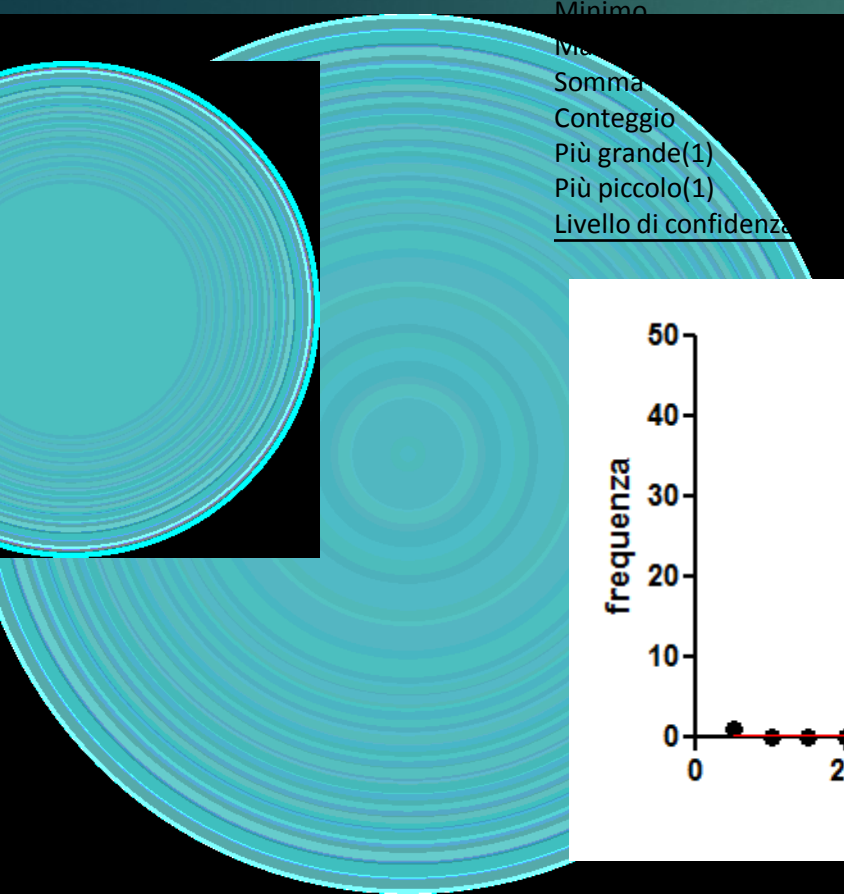
Hct 139 DOGS

Hct	
Media	41,37116
Errore standard	0,626669
Mediana	42,15
Moda	45,4
Deviazione standard	7,361699
Varianza campionaria	54,19461
Curtosi	3,452818
Asimmetria	-0,96729
Intervallo	52,58
Minimo	4,82
Maximo	57,4
Somma	5709,22
Conteggio	138
Più grande(1)	57,4
Più piccolo(1)	4,82
Livello di confidenza (95%)	1,239196



Goodness of Fit:

$R^2 = 0,9724$



MISURA DELLA TENDENZA CENTRALE

27

ARITHMETIC MEAN

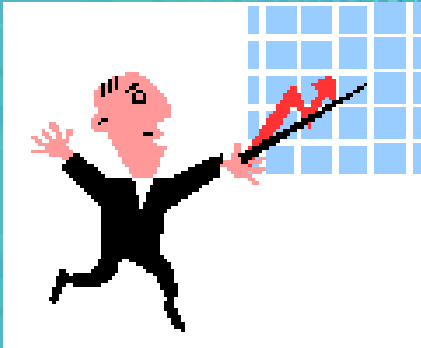
The arithmetic mean (or simply "mean") of a sample, usually denoted by \bar{x} , is the sum of the sampled values divided by the number of items in the sample

MEDIAN

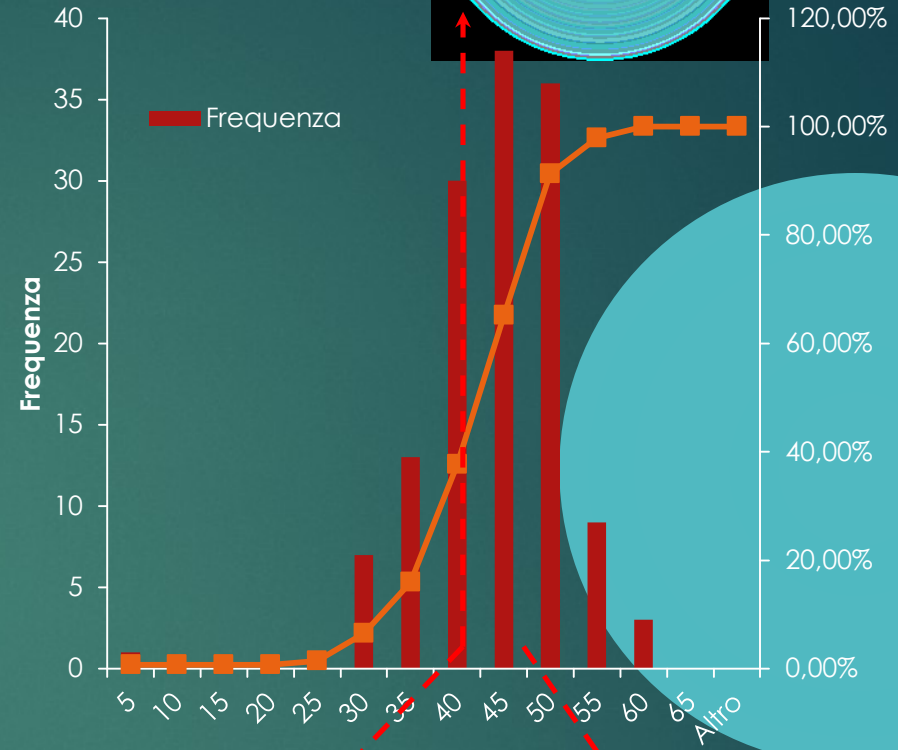
The **median** is the value separating the higher half of a data sample, a population, or a probability distribution, from the lower half.

MODE

The **mode** of a set of data values is the value that appears most often

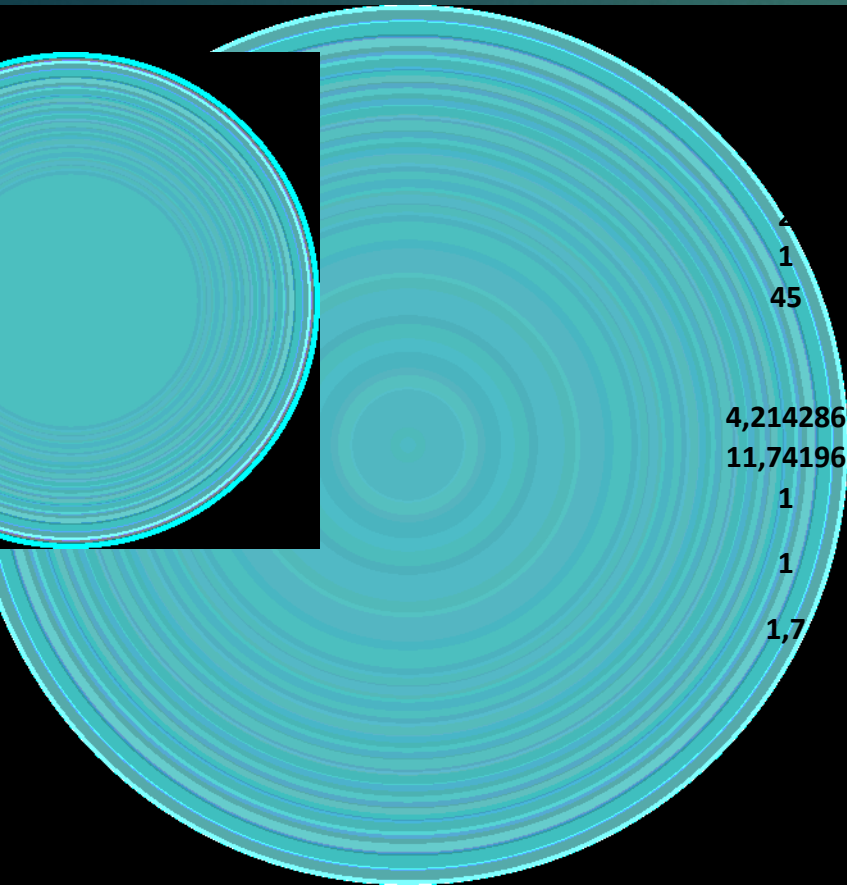


Hct	
Media	41,37116
Errore standard	0,626669
Mediana	42,15
Moda	45,4
Deviazione	7,361699
Varianza camp	54,19461
Curtosi	3,452818
Asimmetria	-0,96729
Intervallo	52,58
Minimo	4,82
Massimo	57,4
Somma	5709,22
Conteggio	138
Più grande(1)	57,4
Più piccolo(1)	4,82
Livello di confidenza(95,0%)	1,239196



median

mode

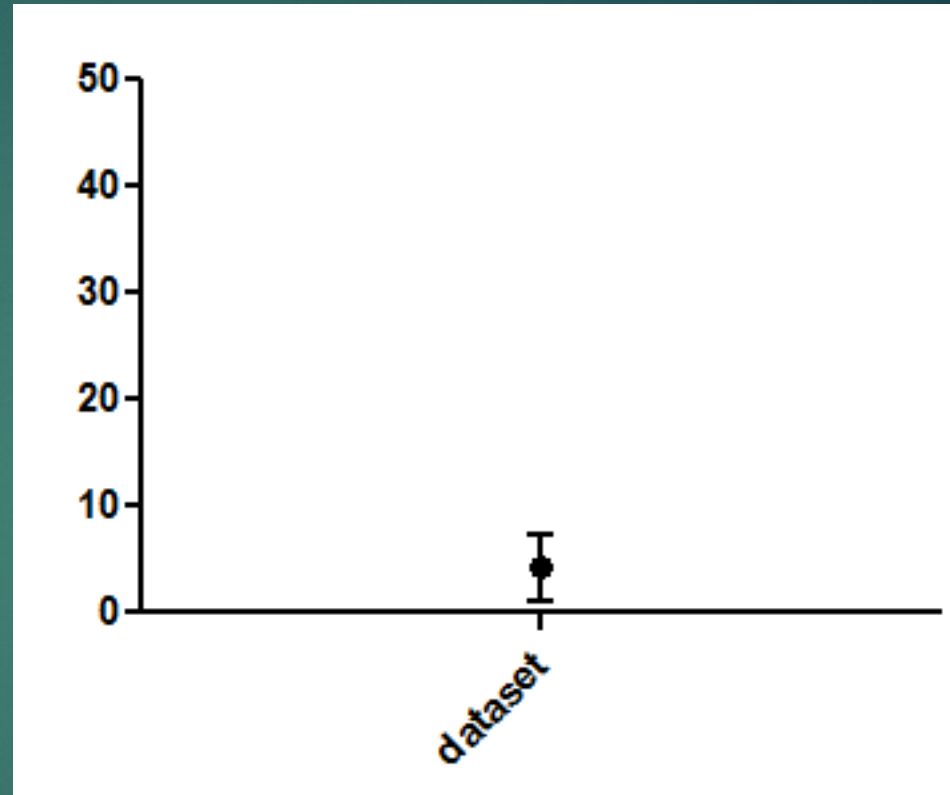


dataset

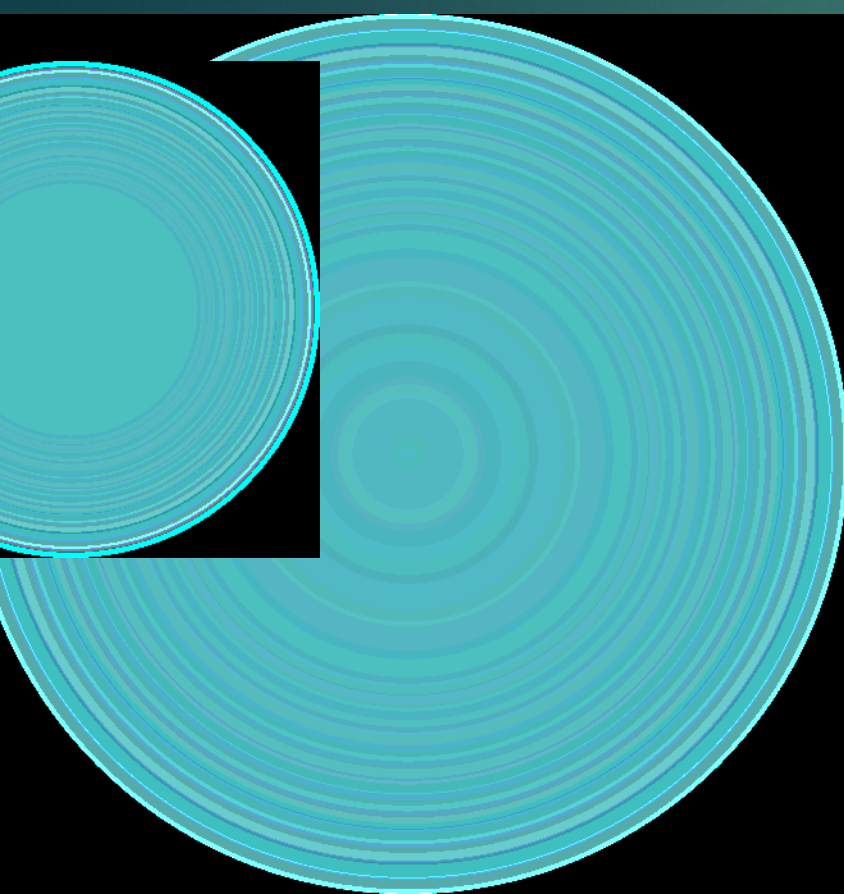
1
1
1
1
1
1

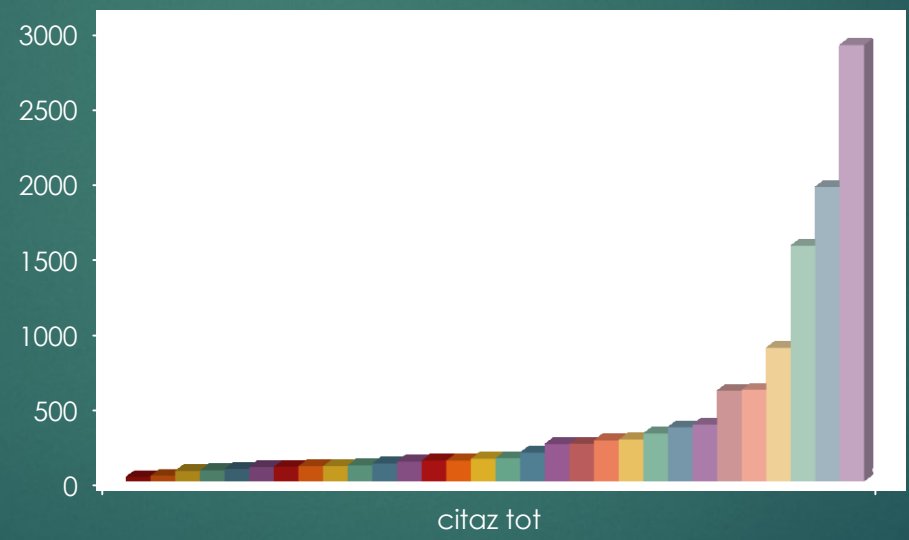
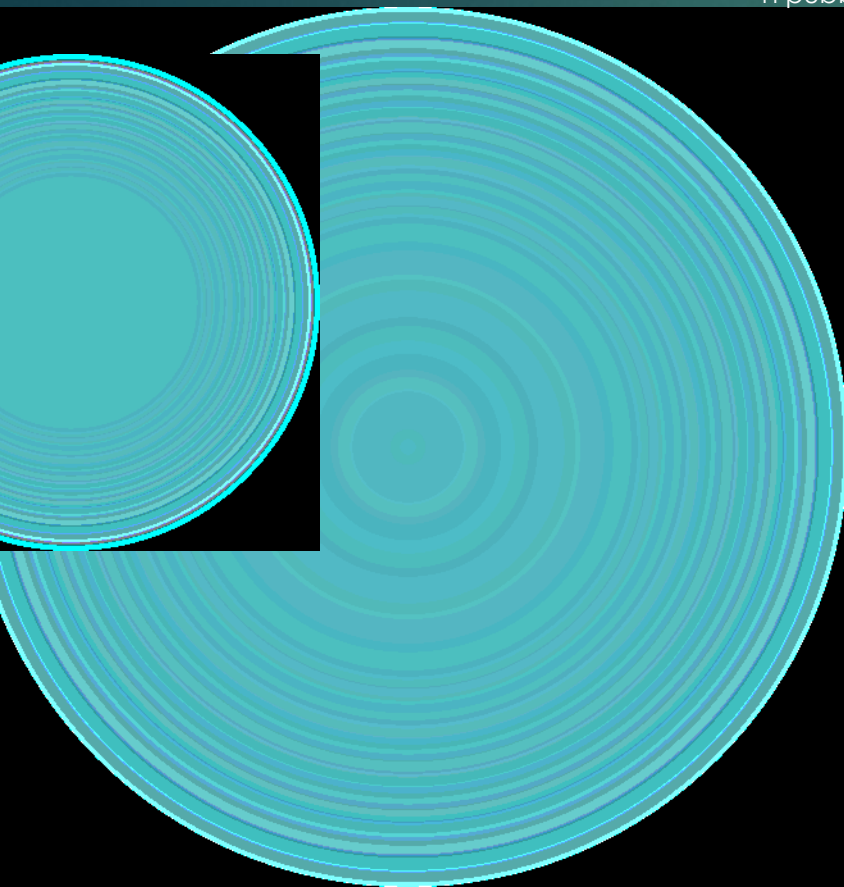
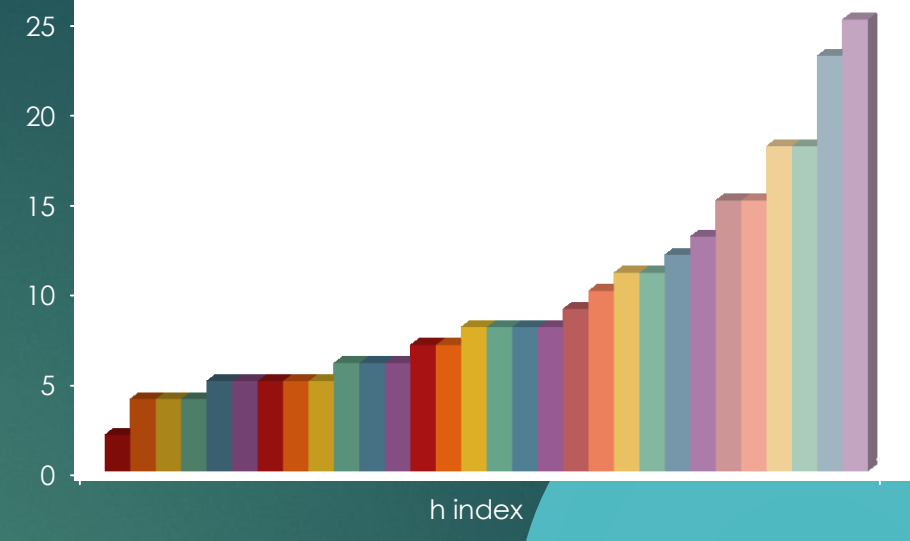
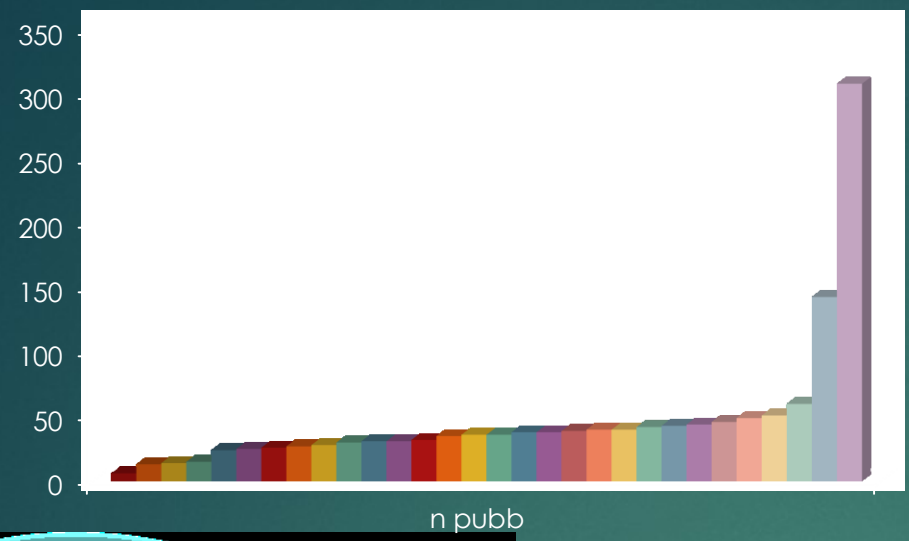
4,214286
11,74196
1
1
1,7

media
ds
mediana
10°percentile
90°percentile



Autore	n pubb	h index	citaz tot
1	36	5	117
2	36	6	96
3	49	12	317
4	25	5	130
5	27	10	247
6	51	18	1565
7	60	18	888
8	143	23	1955
9	42	11	271
10	30	8	153
11	31	7	149
12	46	8	189
13	308	25	2895
14	39	5	100
15	6	2	67
16	24	4	28
17	14	6	72
18	13	4	37
19	40	8	249
20	15	4	277
21	32	11	377
22	43	15	609
23	38	8	137
24	28	5	81
25	44	13	603
26	31	9	105
27	26	6	94
28	40	15	359
29	38	7	137
30	35	5	100

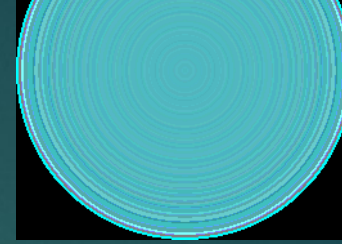




	n pubb	h index	citaz tot
mediana	36,0	8,0	151,0
media	46,3	9,4	413,5



MISURA DELLA VARIABILITA'



32

VARIANZA

$$\frac{\sum (x - \bar{x})^2}{(n - 1)}$$

= σ^2

DEVIAZIONE STANDARD

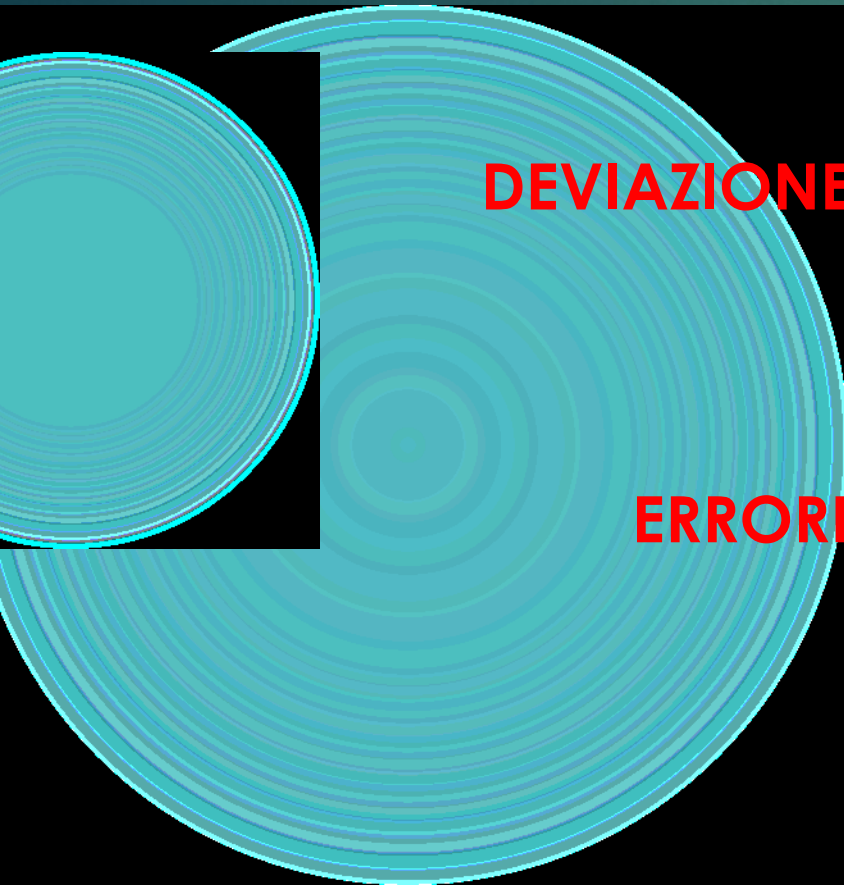
$$\sqrt{\frac{\sum (x - \bar{x})^2}{(n - 1)}}$$

= σ

ERRORE STANDARD

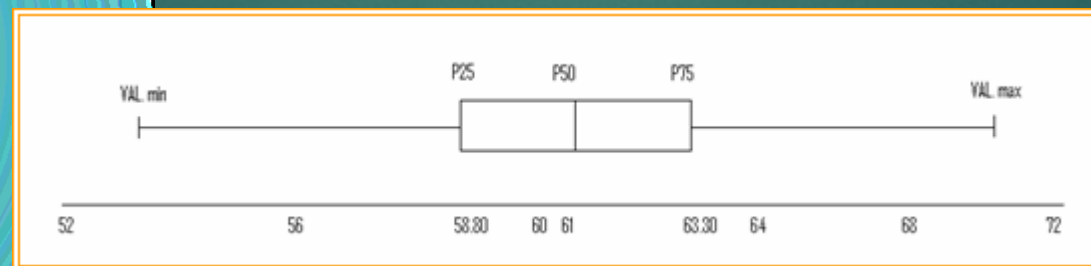
$$\sigma / \sqrt{n}$$

PERCENTILE



Percentiles

box plot



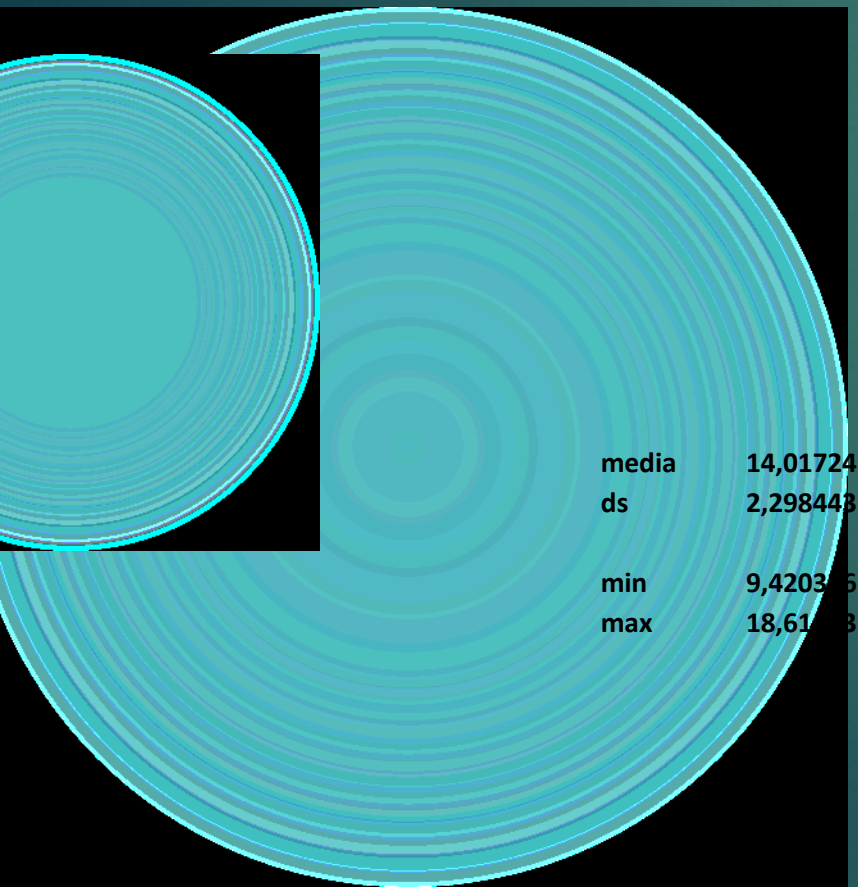
REFERENCE INTERVALS

34

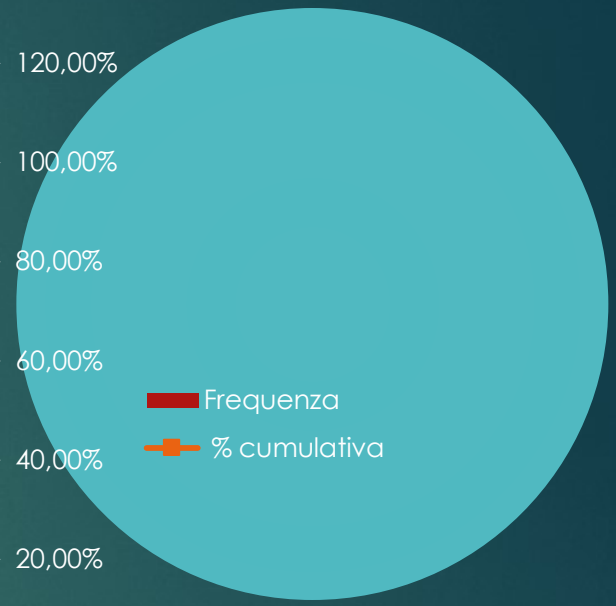
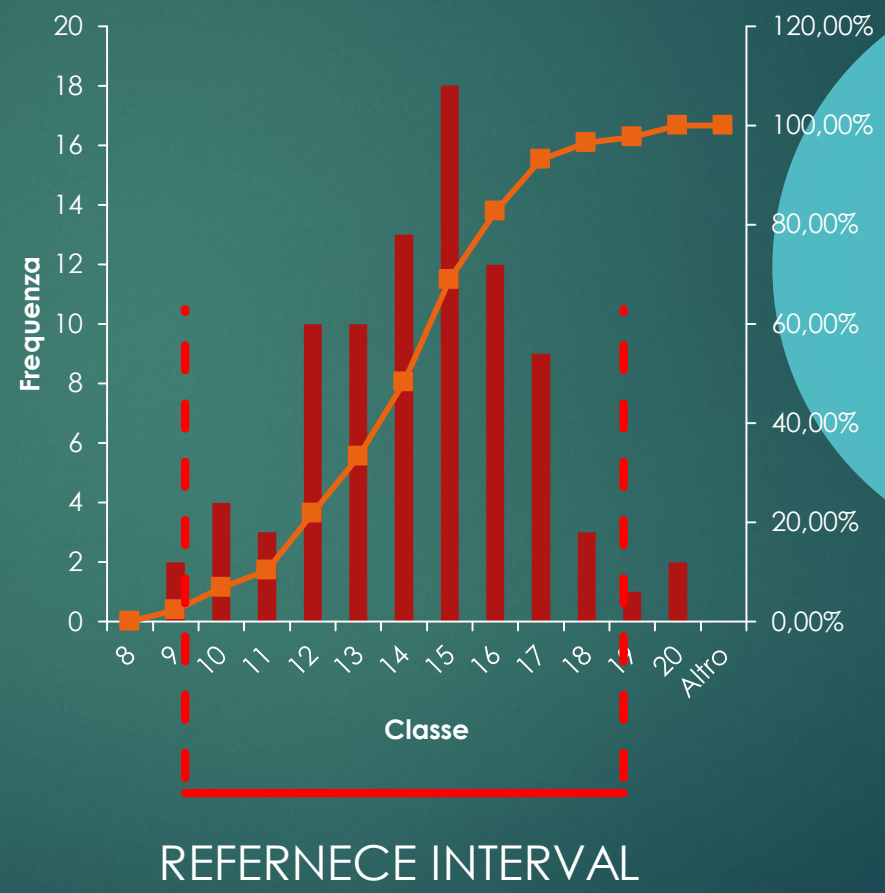
Reference ranges represent the range of values that includes 95% of the observed results in a healthy subjects control group.

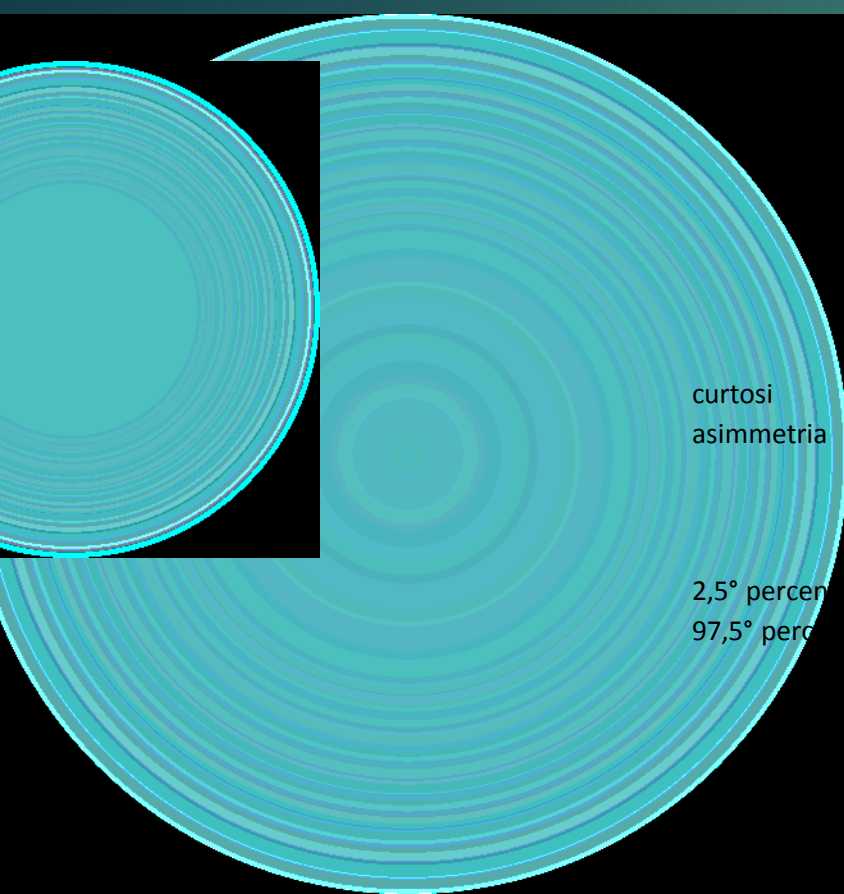


Hgb



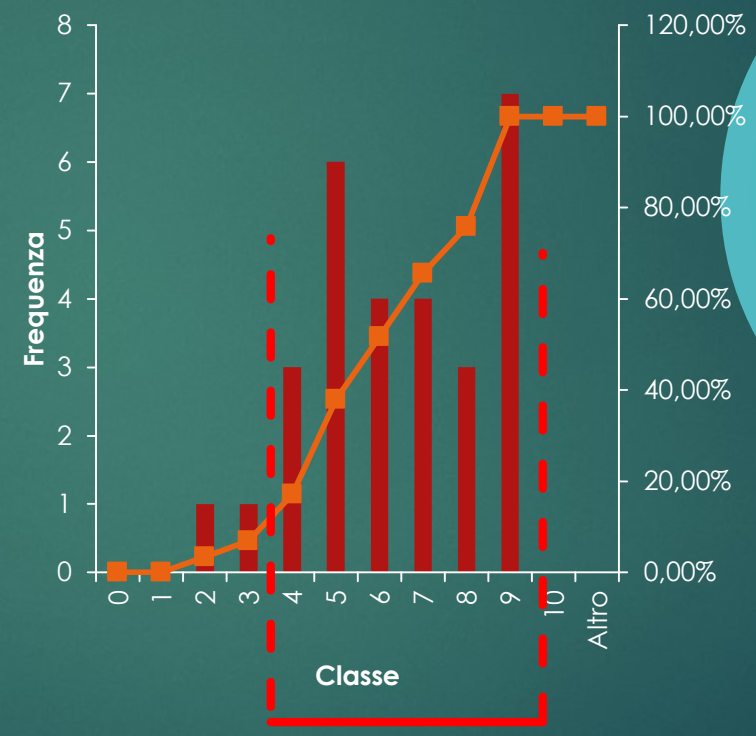
media 14,01724
ds 2,298443
min 9,420356
max 18,61123





curtosi -0,88313
 asimmetria -0,23046

2,5° percentile 3,4
 97,5° percentile 9



REFERENCE INTERVAL



A healthy subject undergoing a laboratory analysis has 95% chance that their value will be within the reference ranges;



A healthy subject undergoing 20 laboratory analyzes has a probability of $(0.95)^{20} = 0.358486$ that all results fall within the reference intervals. That is, up to 100 healthy subjects performing each of 20 analyzes, only around 36% will have all values within the reference intervals.