# **Random networks**



Image 3.1 From a cocktail party to random networks.



# Erdős-Rényi model

sets an edge between each pair of nodes with equal probability, independently of the other edges G(n,p)



- 1. Start with N isolated nodes.
- Select a node pair, and generate a random number between o and 1. If the random number exceeds *p*, connect the selected node pair with a link, otherwise leave them disconnected.
- 3. Repeat step (2) for each of the N(N-1)/2 node pairs.

# Random networks









Image 3.22a Water-Ice phase transition.

The hydrogen bonds that hold the water molecules together (dotted lines) are weak, constantly breaking up and re-forming, maintaining partially ordered local structures (left panel). The temperature-pressure phase diagram indicates (center panel) that by lowering the temperature, the water undergoes a phase transition, moving from a liquid (orange) to a frozen solid (red). In the solid phase each water molecule binds rigidly to four other molecules, forming an ice lattice (right panel). After <a href="http://www.lbl.gov/Science-Articles/Archive/sabl/2005/February/water-solid.html">http://www.lbl.gov/Science-Articles/Archive/sabl/2005/February/water-solid.html</a>; phase diagram after <a href="http://stevengoddard.wordpress.com/2010/09/02/the-ideal-world-phase-diagrams-part-deux/">http://stevengoddard.wordpress.com/2010/09/02/the-ideal-world-phase-diagrams-part-deux/</a>.







Image 3.4b Degree distribution is independent of the network size.





(a) The relative size of the giant component in function of the average degree *k* in the Erdős-Rényi model.
(b)-(e) The main network characteristics in the four regimes that characterize a random network.

# Watts and Strogatz model

- However the <u>ER</u> graphs do not have two important properties observed in many real-world networks:
- They do not generate local clustering and triadic closures. Instead because they have a constant, random, and independent probability of two nodes being connected, ER graphs have a low clustering coefficient.

# Small world





#### Image 3.9

#### Six degrees of separation.

According to six degrees of separation any two individuals, anywhere in the world, can be connected through a chain of six or fewer acquaintances. This means that while Sarah does not know Peter, she knows Ralph, who knows Jane and who in turn knows Peter. Hence Sarah is three degrees from Peter. In the language of network science six degrees, also called the small world property, states that the distance between any two nodes in a network is unexpectedly small.



Image 3.13 Stanley Milgram (1933-1984)

# Six degree of separation

### Milgram experiment





# Small wolrd









#### Image 3.11

#### Six degrees? Facebook finds only four.

Milgram's experiment could not detect the true distance between his study's participants, as he lacked an accurate map of the full social network. Today Facebook has the most extensive social network map ever assembled. Using Facebook's social graph of May 2011, consisting of 721 million active users and 68 billion symmetric friendship links, the average distance between the users was 4.74. The figure shows the distance distribution,  $p_{a}$ , for all pairs of Facebook users worldwide (full dataset) and within the US only. Therefore, instead of 'six degrees' researchers detected only 'four degrees of separation' [4], closer to the prediction of Eq. (20) than to Milgram's six degrees [23]. Using Facebook's *N* and *L* Eq. (19) predicts the average degree to be approximately 3.90, not far from the reported four degrees.

# WS networks: node degree



$$P(k) = \sum_{n=0}^{f(k,K)} C_{K/2}^n \left(1-\beta\right)^n \beta^{K/2-n} \frac{(\beta K/2)^{k-K/2-n}}{(k-K/2-n)!} e^{-\beta K/2}$$

# Small-world network

Specifically, a small-world network is defined to be a network where the typical distance *L* between two randomly chosen nodes (the number of steps required) grows proportionally to the logarithm of the number of nodes*N* in the network, that is:<sup>[1]</sup>

 $L \propto \log N$ 

# The hubs



# Barabasi-Albert model

• Node degree:  $\mathbf{y} = \mathbf{a} \mathbf{x}^{-\mathbf{b}}$ 



# WWW









# Robustness against random attacks

Scale-Free Network, Accidental Node Failure





Scale-Free Network, Attack on Hubs







# Hierarchical networks



# ... in conclusion





**Figure 1** | **Modelling a blackout in Italy.** Illustration of an iterative process of a cascade of failures using real-world data from a power network (located on the map of Italy) and an Internet network (shifted above the map) that were implicated in an electrical blackout that occurred in Italy in September 2003<sup>20</sup>. The networks are drawn using the real geographical locations and every Internet server is connected to the geographically nearest power station. **a**, One power station is removed (red node on map) from the power network and as a result the Internet nodes depending on it are removed from the Internet network (red nodes above the map). The nodes that will be disconnected from the giant cluster (a cluster that spans the entire network)

at the next step are marked in green. **b**, Additional nodes that were disconnected from the Internet communication network giant component are removed (red nodes above map). As a result the power stations depending on them are removed from the power network (red nodes on map). Again, the nodes that will be disconnected from the giant cluster at the next step are marked in green. **c**, Additional nodes that were disconnected from the giant component of the power network are removed (red nodes on map) as well as the nodes in the Internet network that depend on them (red nodes above map).

# In physiology...



#### Figure 2. Networks in Cellular Systems

To date, cellular networks are most available for the "super-model" organisms (Davis, 2004) yeast, worm, fly, and plant. High-throughput interactome mapping relies upon genome-scale resources such as ORFeome resources. Several types of interactome networks discussed are depicted. In a protein interaction network, nodes represent proteins and edges represent physical interactions. In a transcriptional regulatory network, nodes represent transcription factors (circular nodes) or putative DNA regulatory elements (diamond nodes); and edges represent physical binding between the two. In a disease network, nodes represent diseases, and edges represent gene mutations of which are associated with the linked diseases. In a virus-host network, nodes represent viral proteins (square nodes) or host proteins (round nodes), and edges represent physical interactions between the two. In a metabolic network, nodes represent enzymes, and edges represent metabolites that are products or substrates of the enzymes. The network depictions seem dense, but they represent only small portions of available interactome network maps, which themselves constitute only a few percent of the complete interactomes within cells.

# Come si costruisce una rete?

Si parte da un database

- depositato e certificato
- creato ad hoc

# Archives on line









WIKIPATHWAYS Pathways for the People

## For instance...



# or....xls o .xlsx

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# Network creation and analysis













# File formats

•Simple interaction file (SIF or .sif format)

- •Graph Markup Language (GML or .gml format)
- •XGMML (extensible graph markup and modelling language).

•SBML

•BioPAX

•PSI-MI Level 1 and 2.5

•Delimited text

•Excel Workbook (.xls)

# Network realization I



# Network realization II



# Network realization III



## Layout



# Layout II



# Layout III



# Layout IV

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# Analysis



# Analysis

